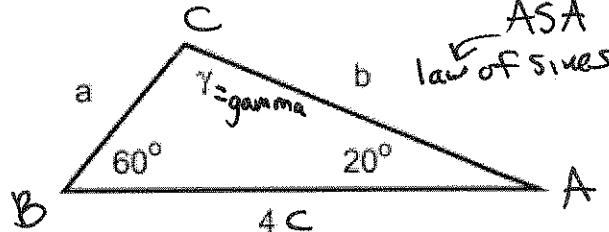


Unit 5 Test Review – Common Core Math 2 Honors

1. Find the remaining sides and angle in the following triangle:



$$\textcircled{1} \quad 180 - 60 - 20 = 100 \quad \begin{array}{l} B \\ A \end{array} \quad \begin{array}{l} 100 \\ C = \gamma \end{array} \quad \text{gamma}$$

$$\textcircled{2} \quad \frac{\sin(100)}{4} = \frac{\sin(20)}{a}$$

$$\frac{a \sin(100)}{\sin(20)} = \frac{4 \sin(20)}{\sin(100)} \quad \boxed{a = 1.4}$$

$$\textcircled{3} \quad \frac{\sin(100)}{4} = \frac{\sin(60)}{b}$$

$$\frac{b \sin(100)}{\sin(60)} = \frac{4 \sin(60)}{\sin(100)} \quad \boxed{b = 3.5}$$

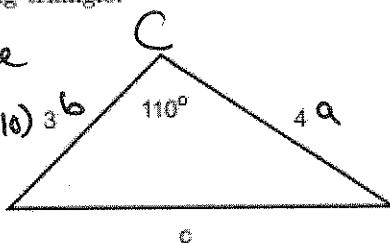
2. Find the third side of the following triangle:

SAS  $\rightarrow$  Law of Cosine

$$c^2 = 4^2 + 3^2 - 2(4)(3)\cos(110) \quad \begin{array}{l} 4 \\ 3 \end{array} \quad \begin{array}{l} b \\ a \end{array}$$

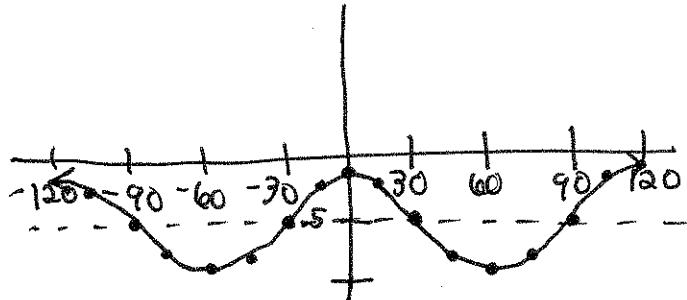
$$c^2 = 33.21$$

$$c = 5.8$$

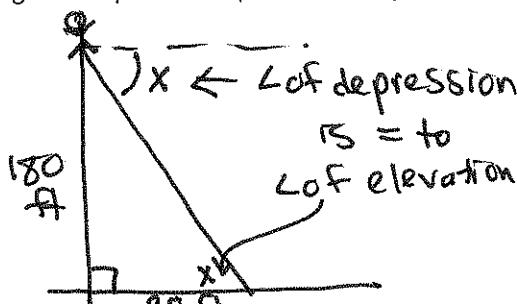


3. For the function  $y = -5 + 4\cos(3x)$   $\Rightarrow y = 4\cos(3x) - 5$

- a. The amplitude.  $|4| = 4 = |a|$
- b. The period.  $\pi r = 360/3 \quad 120^\circ = 360/b$
- c. The equation of the midline.  $y = -5 = d$
- d. Graph 1 period in the negative and positive directions.



4. A building 180 feet tall casts a 90 foot long shadow. If a person looks down from the top of the building, what is the measure of the angle of depression? (Assume the person's eyes are level with the top of the building.)



$$\tan(x) = \frac{180}{90}$$

$$x = \tan^{-1}\left(\frac{180}{90}\right)$$

$$x = 63.4^\circ$$

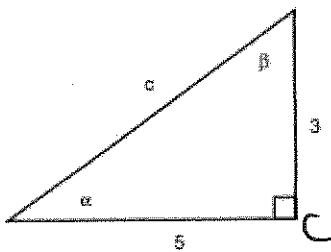
Pythagorean thm.

5. Solve the right triangle, finding the angles in degrees to at least 3 decimal places.

$$\textcircled{1} \quad \tan(\alpha) = \frac{3}{5}$$

$$\alpha = \tan^{-1}(3/5)$$

$$\alpha = 30.964^\circ$$



$$\textcircled{2} \quad 180$$

$$-90 C$$

$$-30.964 \alpha$$

$$59.036 = \beta$$

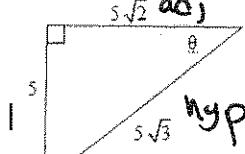
$$\textcircled{3} \quad 3^2 + 5^2 = c^2$$

$$\sqrt{34} = c$$

$$c = 5.831$$

6.

A. Find  $\cos \theta$



CAH

$$\cos \theta = \frac{5\sqrt{2}}{5\sqrt{3}} = \frac{\sqrt{2} \cdot \sqrt{3}}{\sqrt{3} \cdot \sqrt{3}}$$

$$\cos \theta = .816$$

$$= \frac{\sqrt{6}}{3}$$

B. Find  $\sin \theta$ 

$$\sin \theta = \frac{5}{13}$$

C. Find  $\tan \theta$ 

$$\begin{aligned} ① 6^2 + y^2 &= 9^2 && \text{Pythagorean Theorem} \\ y^2 &= 45 \\ y &= 3\sqrt{5} \\ ② T^o A & \end{aligned}$$

D. Find  $\sin \theta$ 

$$\begin{aligned} \tan \theta &= \frac{6}{3\sqrt{5}} = \frac{2}{\sqrt{5}} \cdot \frac{\sqrt{5}}{\sqrt{5}} = \frac{2\sqrt{5}}{5} \\ \text{hyp} & \\ x & \text{ opp} \\ 7 & \end{aligned}$$

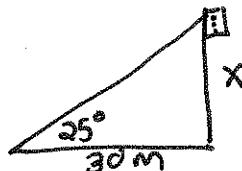
$$① 7^2 + x^2 = 25^2$$

$$x = 24$$

$$② 5^o +$$

$$\sin \theta = \frac{x}{25} = \boxed{\frac{24}{25}}$$

7. A person is standing 30 meters from a traffic light. If the angle of elevation from the person's feet to the top of the traffic light is 25 degrees, find the height of the traffic light.

T<sup>o</sup> A

$$\tan(25) = \frac{x}{30}$$

$$x = 30 \tan(25) = 13.989$$

$$\approx 14 \text{ m}$$

8. Find all solutions to  $2 \sin 2x + 1 = 0$  for  $0 \leq x \leq 2\pi$ .

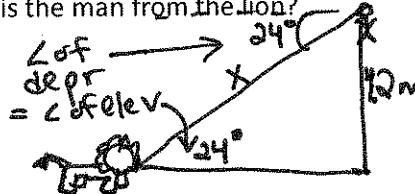
$$\begin{aligned} -1 - 1 \\ \frac{2 \sin 2x}{2} = -\frac{1}{2} \\ \sin 2x = -\frac{1}{2} \end{aligned}$$

$$\rightarrow \sin^{-1}(\sin 2x) = \sin^{-1}(-\frac{1}{2})$$

$$\frac{2x}{2} = -30$$

$$x = -15$$

9. From the top of a fence, a person sites a lion on the ground at an angle of depression of 24 degrees. If the man and the fence is 4.2 meters high, how far is the man from the lion?



$$\sin(24) = \frac{4.2}{x}$$

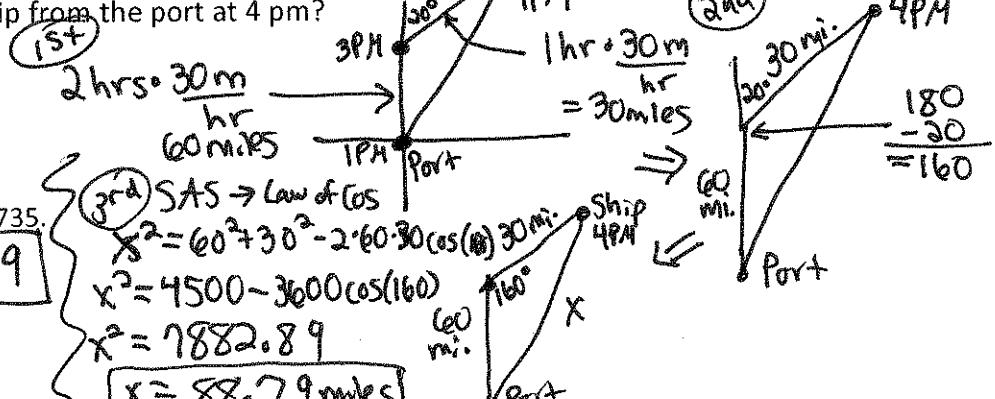
$$x \sin(24) = \frac{4.2}{\sin(24)}$$

$$x = 10.3 \text{ m}$$

10. Find the measure of angle A, to the nearest degree, if  $\sin A = .9659258$ .

$$\begin{aligned} A &= \sin^{-1}(0.9659258) \\ A &= 75^\circ \end{aligned}$$

11. A ship leaves port at 1 pm traveling north at the speed of 30 miles/hour. At 3 pm, the ship adjusts its course on a bearing of N 20° E. How far is the ship from the port at 4 pm?



12. Find the approximate value of  $\tan 735$ .

$$\boxed{.2679}$$

13. Solve the right triangle

① Pyth Thm

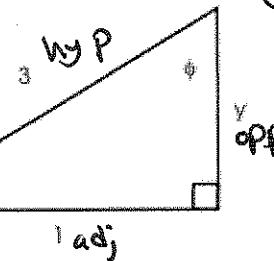
$$x^2 + y^2 = 3^2$$

$$1 + y^2 = 9$$

$$y^2 = 8$$

$$y = \sqrt{8} = \sqrt{4 \cdot 2}$$

$$y = 2\sqrt{2}$$



$$\textcircled{2} \cos \theta = \frac{1}{3}$$

$$\theta = \cos^{-1}(1/3)$$

$$\theta = 70.5^\circ$$

$$\textcircled{3} \quad 180$$

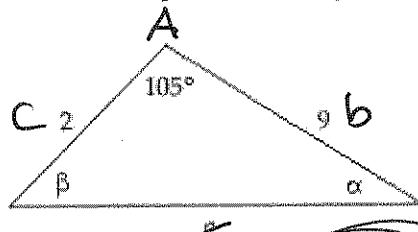
$$- 90$$

$$- 70.5 \theta$$

$$\underline{19.5^\circ = \phi}$$

Find the area of the triangle. If necessary, round the answer to two decimal places.

17)



A) 2.33

**B) 8.69**

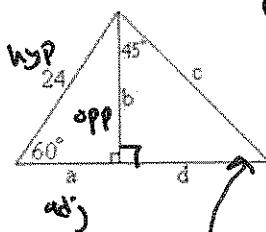
$$\text{Area} = \frac{1}{2} \text{side} \cdot \text{side} \cdot \sin(\text{included angle}) \text{ or } \frac{1}{2} bc \sin A$$

$$= \frac{1}{2}(2)(9) \sin(105)$$

C) 101.42

D) 34.77

23. In the diagram below, find the approximate value of each part labeled with a variable. Show all work.



$$\textcircled{1} \cos(60) = \frac{a}{24}$$

$$a = 24 \cos(60)$$

$$a = 12$$

$$\textcircled{3} 180 - 90 - 45 = 45^\circ$$

$$\textcircled{2} \sin(60) = \frac{b}{24}$$

$$b = 24 \sin(60)$$

$$b = 20.78$$

**4) b = d because isosceles  $\Delta$**

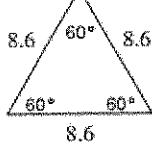
$$d = 20.78$$

$$\textcircled{5} (20.78)^2 + (20.78)^2 = c^2$$

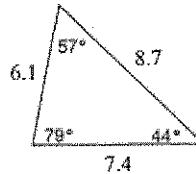
$$\sqrt{864} = c$$

$$c = 29.39$$

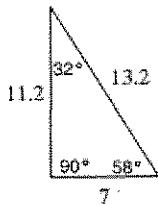
24. Classify each triangle by its sides and its angles:



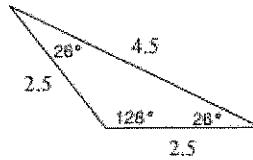
**equilateral  
equiangular  $\Delta$**



**Scalene  
acute  $\Delta$**

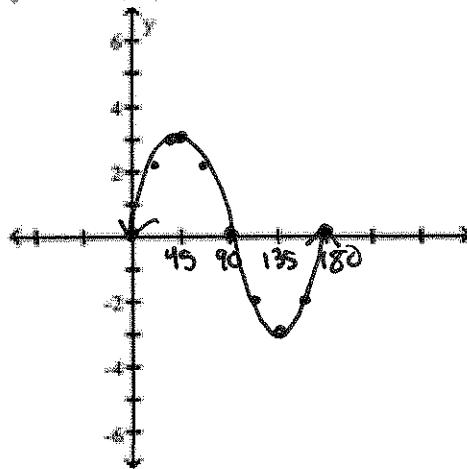


**Scalene  
right  $\Delta$**



**isosceles  
obtuse  $\Delta$**

25.  $y = 3 \sin(2x)$



- Find the midline.
- Find the amplitude.
- Find the period.
- Graph one cycle

$y = 0$	$ a  =$
$\text{amp} = 3$	$ 3  = \text{amp}$
$\text{per} = 180^\circ$	$\text{per} = \frac{360}{2} = 180^\circ$

$$|a| =$$

$$|3| = \text{amp}$$

$$\text{per} = \frac{360}{2} = 180^\circ$$

↳ use calc with  $\text{tbl start} = 0$ ,  $\Delta t b l = 22.5$  to get enough points to see a nice curve

26.  $\sin x \cos x \tan x + \sin x \cos x = 0$

$$\sin x \cos x (\tan x + 1) = 0$$

$$\sin x = 0 \quad \cos x = 0 \quad \tan x + 1 = 0$$

$$x = \sin^{-1}(0) \quad x = \cos^{-1}(0)$$

$$0^\circ \quad 90^\circ$$

$$2 \cos x + 1 = 0$$

$$-1 = -1$$

27.  $2 \cos x (\cos x + \frac{1}{2}) = 0$

$$\frac{2 \cos x}{2} = 0 \quad \cos x + \frac{1}{2} = 0$$

$$-\frac{1}{2} = -\frac{1}{2}$$

$$\cos x = 0$$

$$x = \cos^{-1}(0)$$

$$90^\circ$$

$$\cos x = -\frac{1}{2}$$

$$x = \cos^{-1}(-\frac{1}{2})$$

$$120^\circ$$

28.

$$\frac{2 \cos x}{2} = \frac{1}{2}$$

$$\cos x = \frac{1}{2}$$

$$x = \cos^{-1}(\frac{1}{2})$$

$$60^\circ$$

29. Find  $\sin(15)$  and  $\cos(75)$ . Why is there something special about their values?

$$0.259$$

they are both equivalent values

because their angles are complementary (sum to  $90^\circ$ )