

# Unit 5 Trigonometry Day 8 & 9

## Graphs of Sine and Cosine and Tangent

### Amplitude, Midline, and Period of Sine and Cosine Graphs

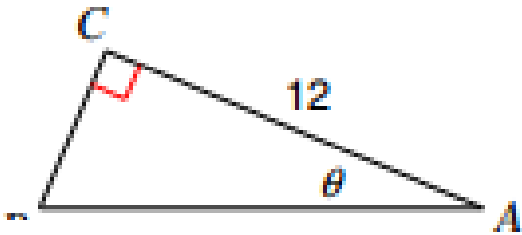
# Unit 5 Trigonometry Day 8

## Introduction to Graphs of Sine and Cosine

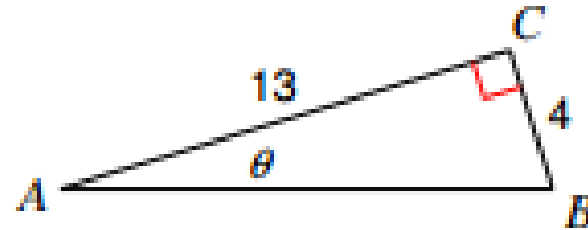
# Warm-Up

Solve for the variable:

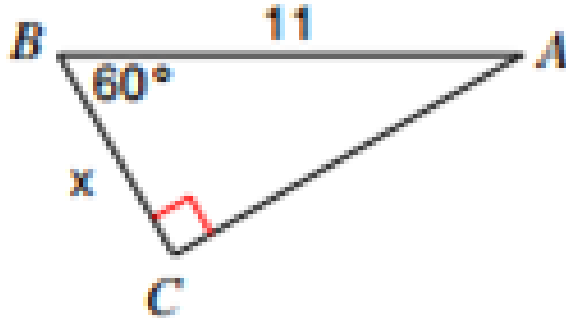
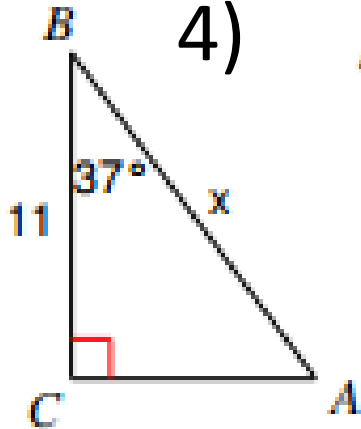
1)



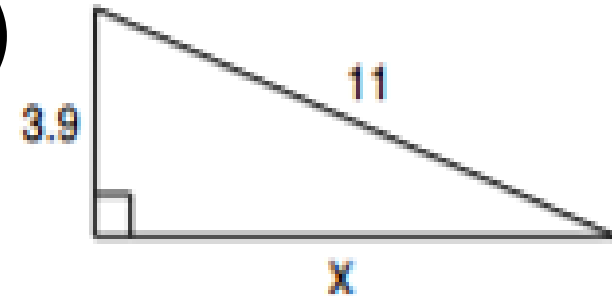
2)



3) 4)



5)



**Add to your notes:**

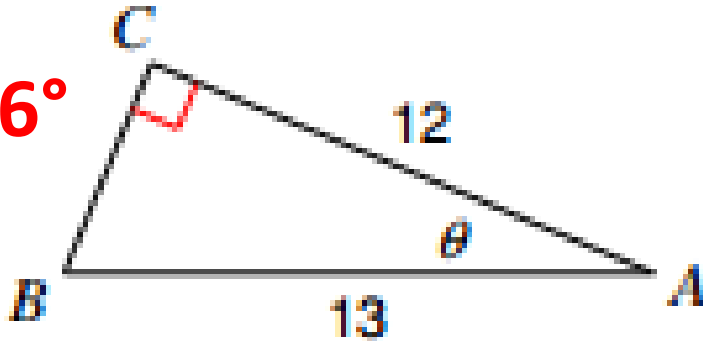
6) The angle of depression from an airplane to the landing strip is  $32^\circ$ . If the plane is at an altitude of 1000 ft, how far does the plane have to travel to get to the landing strip?

# Warm-Up ANSWERS

Solve for the variable:

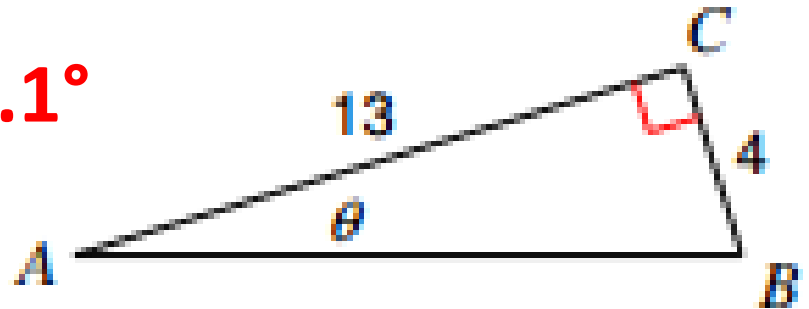
1)

**22.6°**



2)

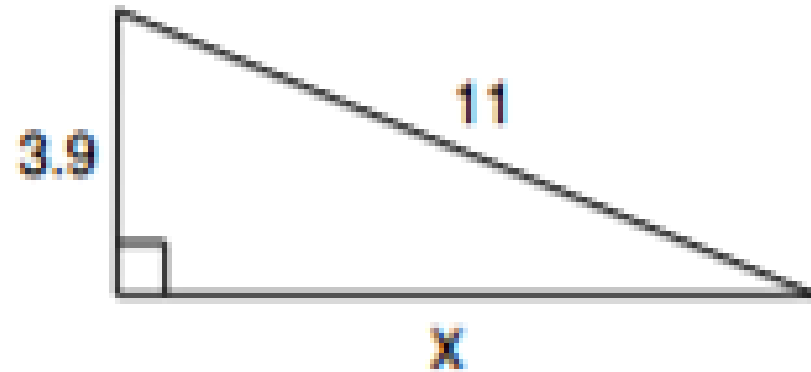
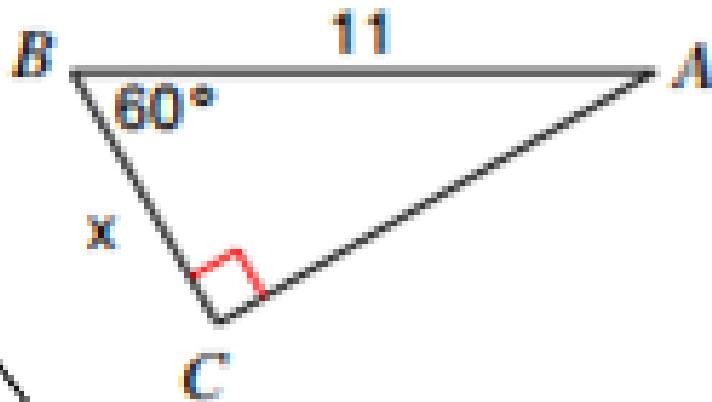
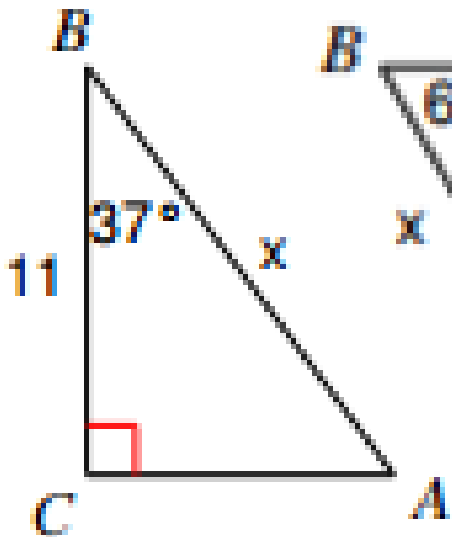
**17.1°**



3) **13.8**

4) **5.5**

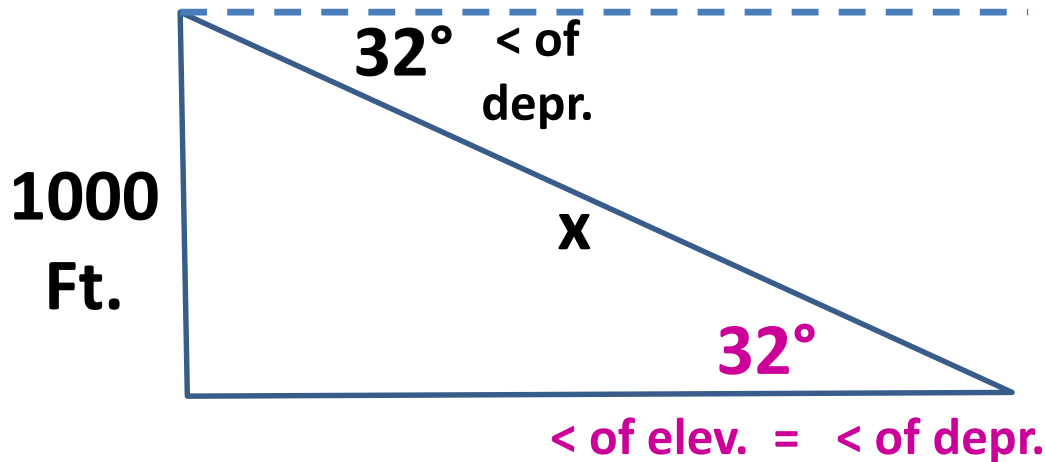
5) **10.3**



# Warm-Up ANSWERS

**Add to your notes:**

6) The angle of depression from an airplane to the landing strip is  $32^\circ$ . If the plane is at an altitude of 1000 ft, how far does the plane have to travel to get to the landing strip?



$$\sin(32^\circ) = \frac{1000}{x}$$

$$x \sin(32^\circ) = 1000$$




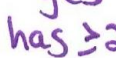
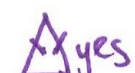




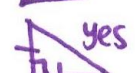



$$x = \frac{1000}{\sin(32^\circ)}$$

**1887.08 ft**

# Homework Answers – Packet p. 15

## Day 6 Homework: Classifying Triangles and their parts

Answer each question with *never*, *sometimes*, or *always*.

1. Right triangles can be obtuse triangles. never
2. Isosceles triangles are equilateral triangles. sometimes →  
3. Equilateral triangles are isosceles triangles. always →     
 *isos Δ has ≥ 2 ≅ sides*
4. Obtuse triangles have more than one obtuse angle. never
5. Equilateral triangles have the same angle measure. always
6. Isosceles triangles are acute triangles. sometimes →  
7. I can use the term *equilateral* when referring to *equiangular* triangles. always
8. Acute triangles are equiangular. sometimes →  
9. Isosceles triangles are right triangles. sometimes →  
10. The angles in scalene triangles are different. always
11. A scalene triangle is an acute triangle. sometimes →   
12. An equilateral triangle is a scalene triangle. never → *can't have = sides + all diff. sides*

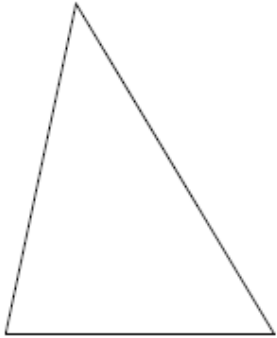
# Homework Answers

Remember to always give 2 names when classifying triangles!

Classify each triangle by its angles and sides. Equal sides and equal angles, if any, are indicated in each diagram.

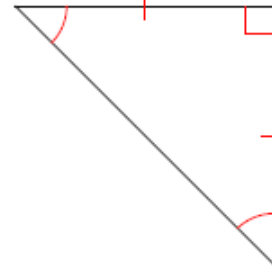
13)

acute scalene



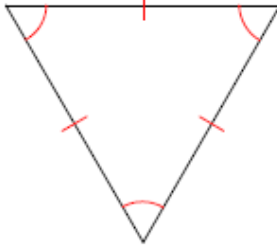
14)

right isosceles



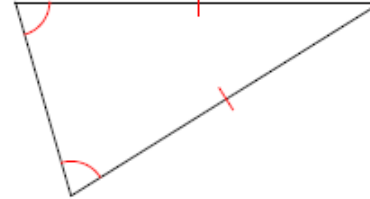
15)

equilateral equiangular



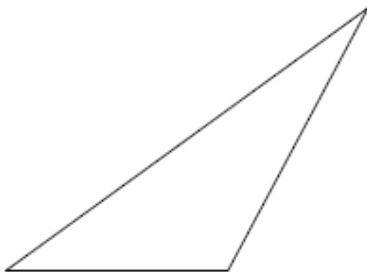
16)

acute isosceles



17)

obtuse scalene



18)

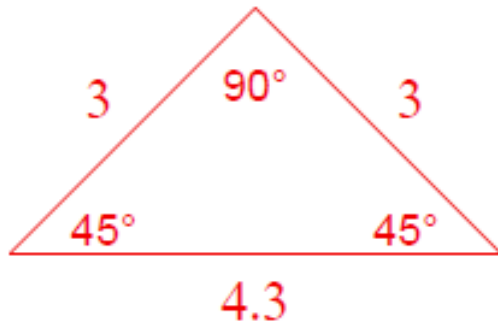
right scalene



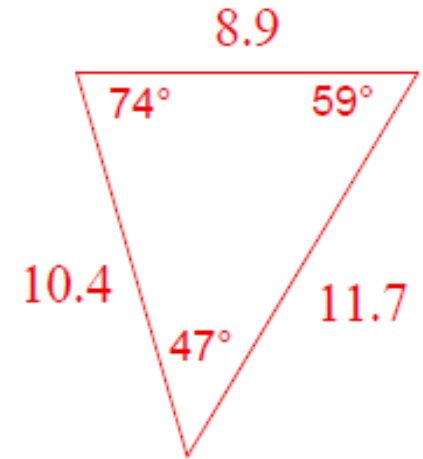
# Homework Answers – Packet p. 16

Sketch an example of the type of triangle described. Label the sides and angles with realistic measurements. If no triangle can be drawn, write "not possible."

19) right isosceles

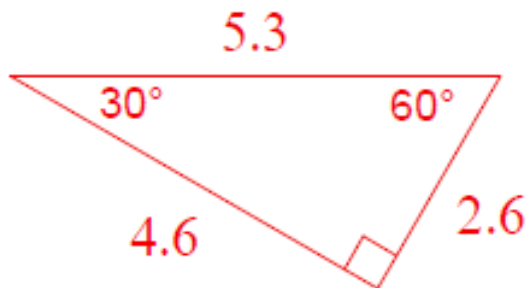


20) acute scalene

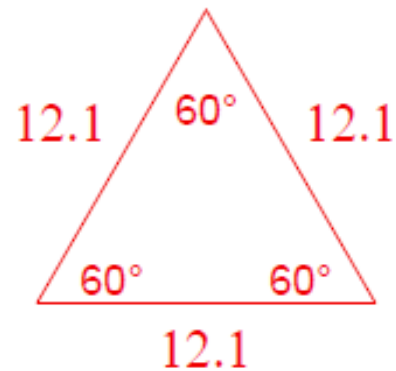


Answers  
will vary! 😊

21) right scalene



22) equilateral

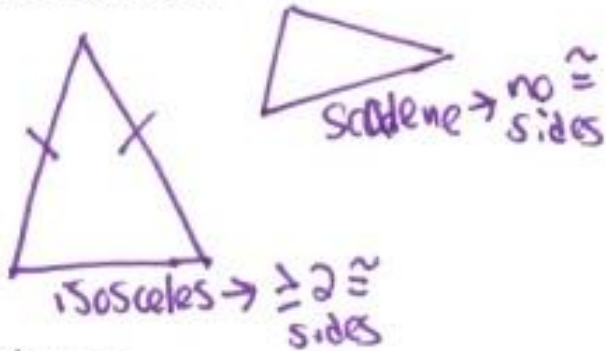




# Homework Answers

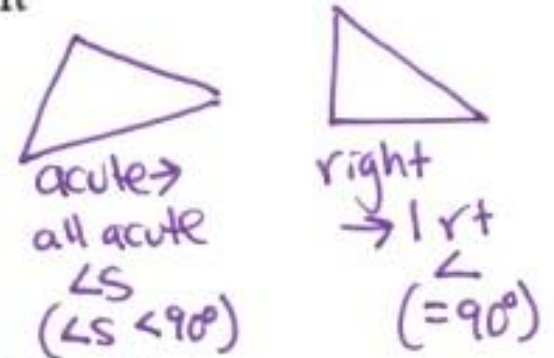
23) scalene isosceles

Not possible



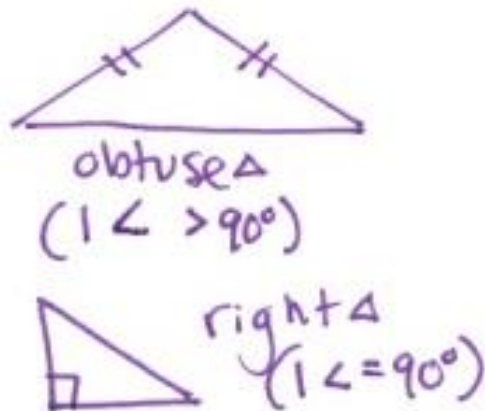
24) acute right

Not possible



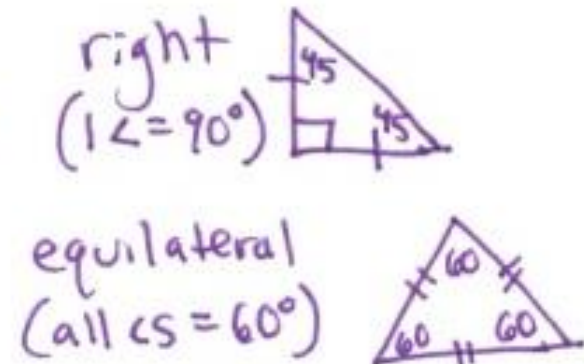
25) right obtuse

Not possible



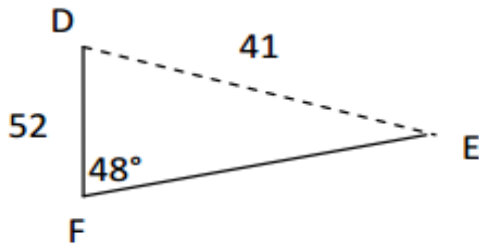
26) right equilateral

Not possible



# HW Answers: Finish Notes p. 14-15

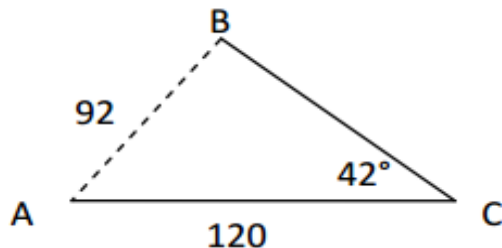
1. For  $\triangle DEF$ ,  
 $e = 52$ ,  $f = 41$ , and  $m\angle F = 48^\circ$ . Find  
all possible  $m\angle E$  to the nearest degree.



$$m\angle E = 70.5^\circ \text{ or } 109.5^\circ$$

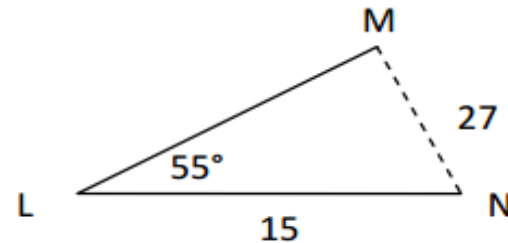
3. For  $\triangle ABC$ ,  
 $b = 120$ ,  $c = 92$ , and  $m\angle C = 42^\circ$ . How  
many triangles can be formed?

2  $\triangle$ s



$$m\angle B = 60.8^\circ \text{ or } 119.2^\circ$$

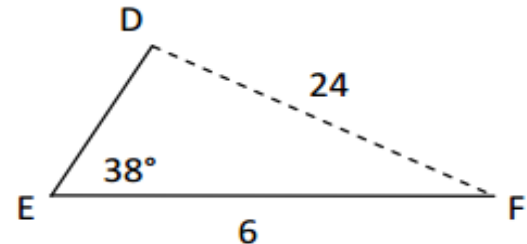
2. For  $\triangle LMN$ ,  
 $l = 27$ ,  $m = 15$ , and  $m\angle L = 55^\circ$ . Find  
all possible  $m\angle M$  to the nearest degree.



$$m\angle M = 27.1^\circ$$

4. For  $\triangle DEF$ ,  
 $d = 6$ ,  $e = 24$ , and  $m\angle E = 38^\circ$ . How  
many Triangles can be formed?

1  $\triangle$



$$m\angle D = 8.9^\circ$$

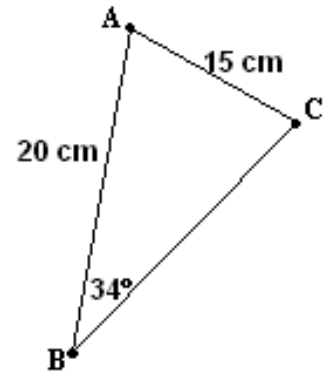
# HW Answers: Finish Notes p. 14-15

5. For triangle DEF,  $d = 25$ ,  $e = 30$ , and  $m\angle E = 40^\circ$ . Find all possible measurements of  $f$  to the nearest whole number.

$$f = 44.48$$

6. Given with ,  $b = 15\text{cm}$ , and , solve the triangle.

Case 1:	Case 2:
$C = 48.21^\circ$	$C = 131.79^\circ$
$A = 97.79^\circ$	$A = 14.21.9^\circ$
$a = 26.58$	$a = 6.58$



7. Given triangle ABC,  $a = 8$ ,  $b = 10$ , and  $m\angle A = 34$ , solve the triangle.

Case 1:	Case 2:
$B = 44.35^\circ$	$B = 135.65^\circ$
$C = 101.65^\circ$	$C = 10.35^\circ$
$c = 14.01$	$c = 2.57$

# Tonight's Homework

Worksheet provided in class

# Notes Day 8

Introduction to Sine and Cosine  
Graphs

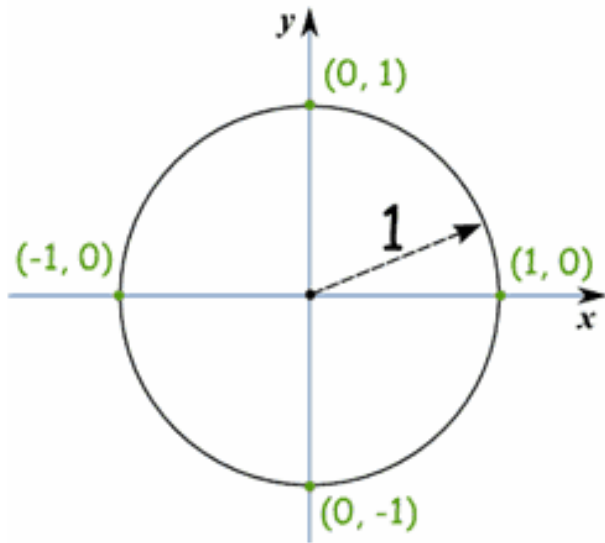
You Need the printed Notes  
AND Notebook Paper

# Graphing Sine & Cosine – basic properties & how they are derived from the Unit Circle

- Use a large Unit Circle to create Sine and Cosine Graphs
- Basic properties of Sine and Cosine Graphs Using the Unit Circle
  - > y in circle = sine values
  - > x in circle = cosine values
  - > angles in the circle are independent variables so they become our x-values on the sine and cosine graphs
  - > sine and cosine values are dependent upon the angle so they become our y-values on the sine and cosine graphs
- Reference the next few slides AND/OR  
Prentice Hall Algebra 2 Blue Textbook
  - > Sine is in Section 13-4 p.720-721
  - > Cosine is in Section 13-5 p.729-730

# The Unit Circle

Not in Notes!  
Just watch! 😊



The "Unit Circle" is a circle with a radius of 1.

Being so simple, it is a great way to learn and talk about lengths and angles.

The center is put on a graph where the x axis and y axis cross, so we get this neat arrangement here.

## Sine, Cosine and Tangent

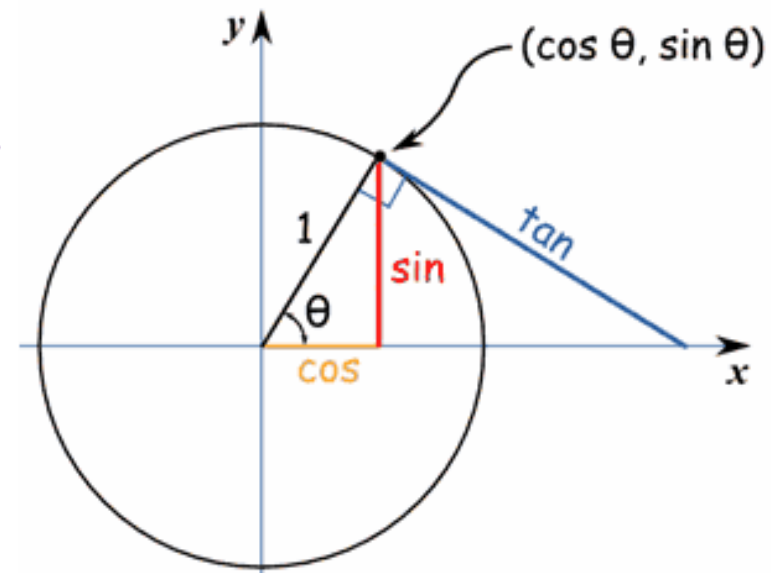
Because the radius is 1, you can directly measure [sine, cosine and tangent](#).

What happens when the angle,  $\theta$ , is  $0^\circ$ ?

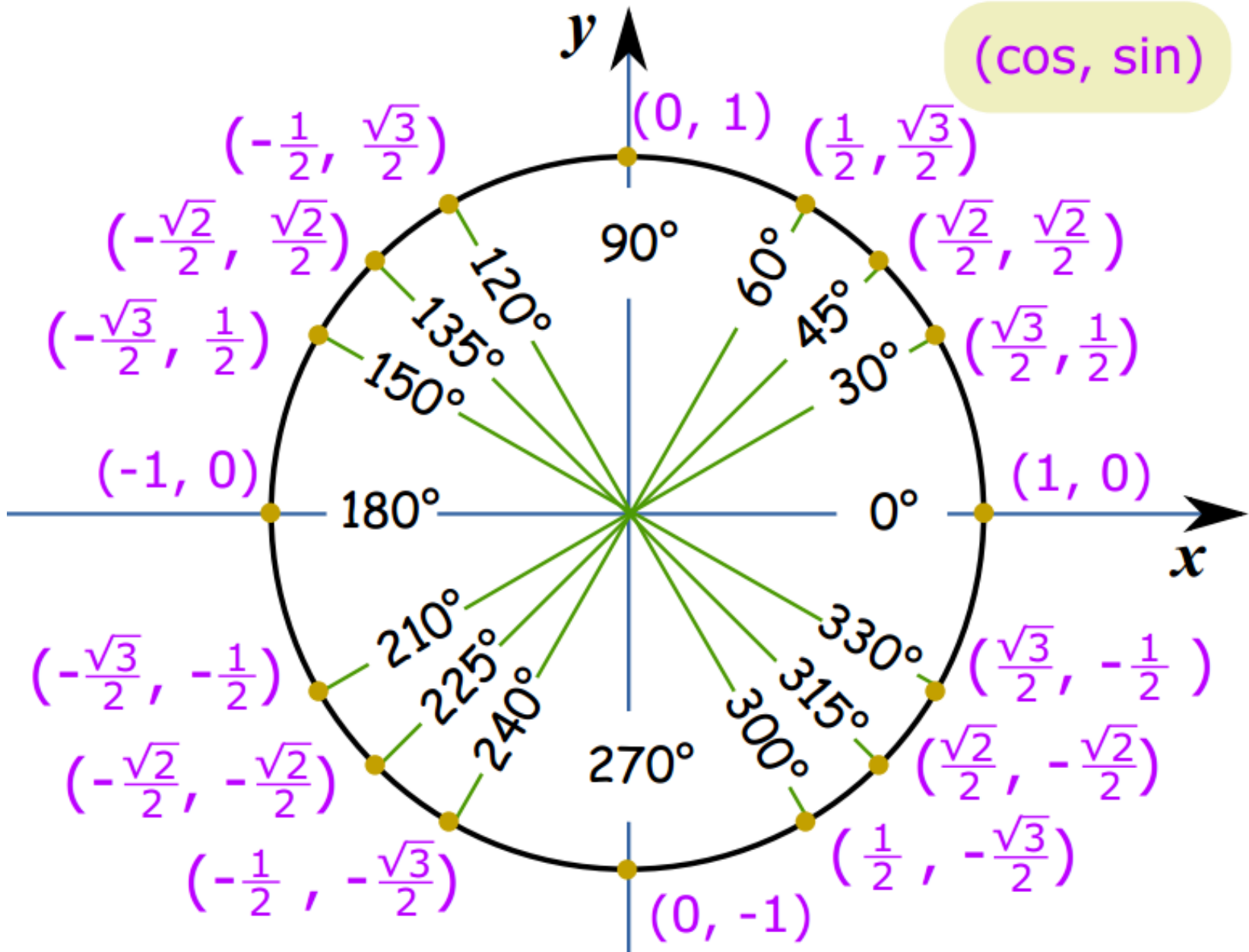
- $\cos 0^\circ = 1$ ,  $\sin 0^\circ = 0$  and  $\tan 0^\circ = 0$

What happens when  $\theta$  is  $90^\circ$ ?

- $\cos 90^\circ = 0$ ,  $\sin 90^\circ = 1$  and  $\tan 90^\circ$  is undefined



Not in Notes! Watch this interactive unit circle 😊





# Day 8 (Monday's) Homework

Worksheet provided in class  
(back of new unit outline)

# Unit 5 Trigonometry Day 9

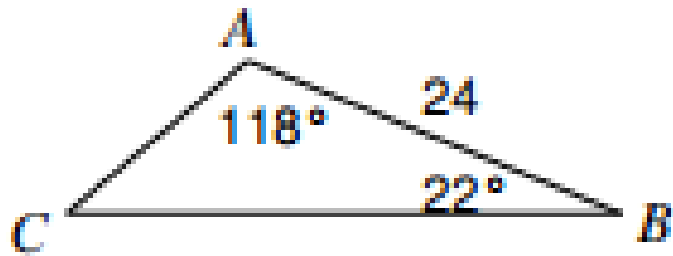
## Graphs of Sine and Cosine and Tangent

### Amplitude, Midline, and Period of Sine and Cosine Graphs

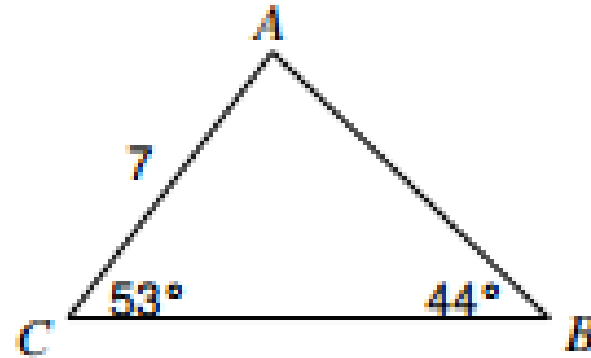
# Day 9 Warm-Up

Find each measurement indicated. Round your answers to the nearest tenth.

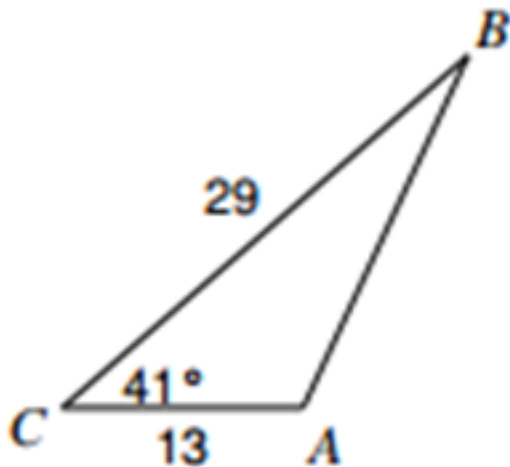
1) Find AC



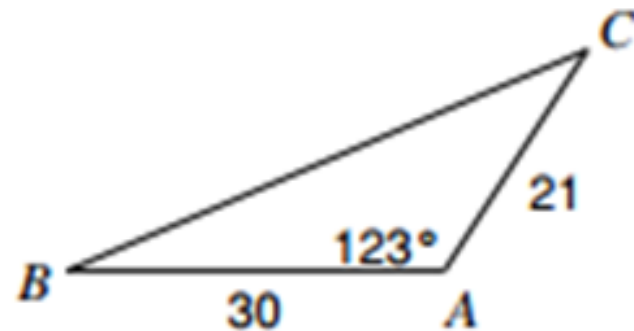
2) Find AB



3) Find AB



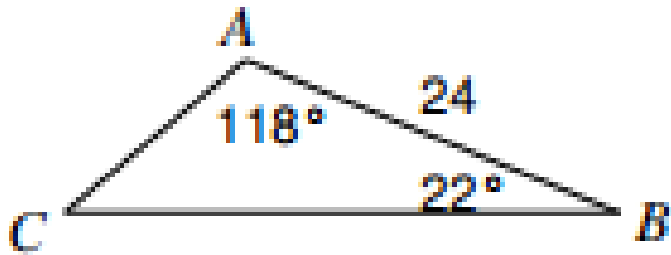
4) Find BC



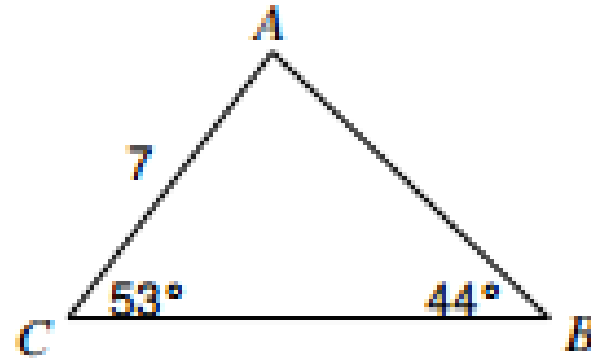
# Day 9 Warm-Up ANSWERS

Find each measurement indicated. Round your answers to the nearest tenth.

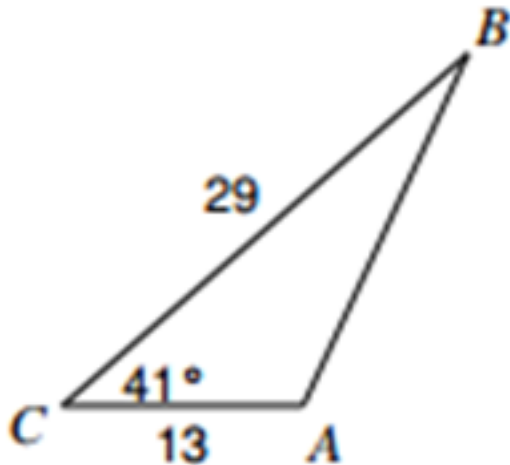
1) Find AC **14**



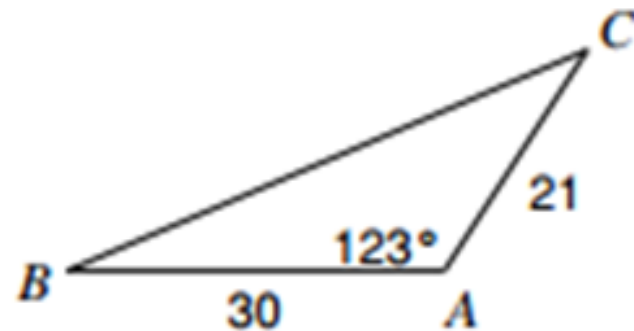
2) Find AB **8**



3) Find AB **21**



4) Find BC **45**



# Notes Day 8 & 9

Let's see how to use the  
calculator to get these graphs!

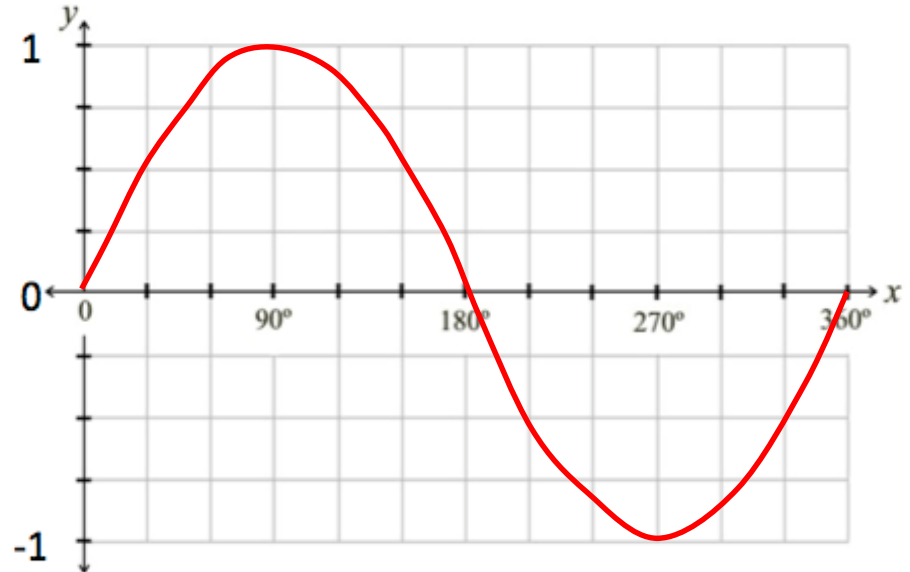
Notes p. 20-22

Complete the table below: Make sure your calculator is in degree mode!!

Degree	$\sin(x)$	Point (Degree, $\sin(x)$ )
0	0	(0,0)
30	0.5	(30, 0.5)
60	0.866	(60, 0.866)
90	1	(90, 1)
120	0.866	(120, 0.866)
150	0.5	(150, 0.5)
180	0	(180,0)
210	-0.5	(210, -0.5)
240	-0.866	(240, -0.866)
270	-1	(270, -1)
300	-0.866	(300, -0.866)
330	-0.5	(330, -0.5)
360	0	(360, 0)

# Graph $\sin(x)$

Notes p. 20

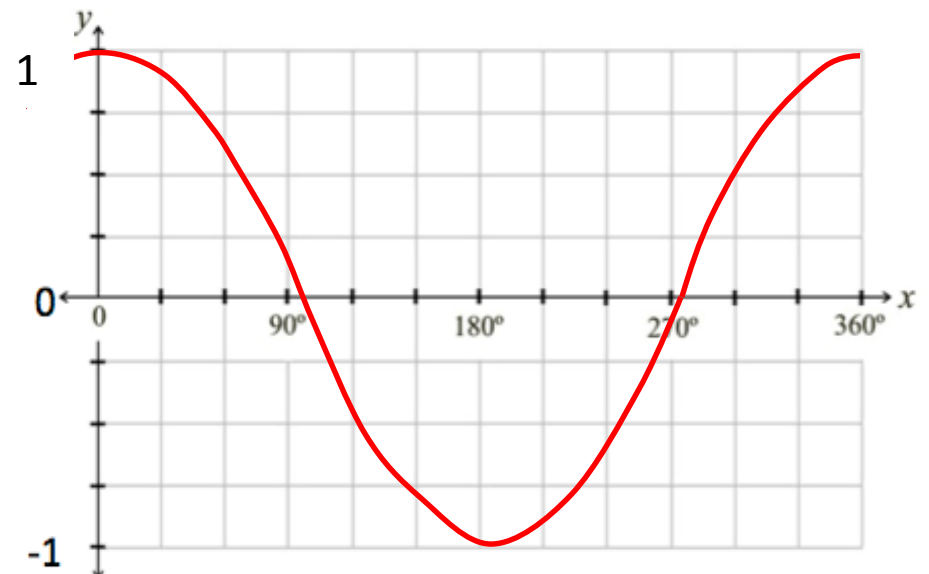


Complete the table below:

Degree	Cos(x)	Point (Degree, Cos(x))
0	1	(0,1)
30	0.866	(30, 0.866)
60	0.5	(60, 0.5)
90	0	(90,0)
120	-0.5	(120, -0.5)
150	-0.866	(150, -0.866)
180	-1	(180, -1)
210	-0.866	(210, -0.866)
240	-0.5	(240, -0.5)
270	0	(270, 0)
300	0.5	(300, 0.5)
330	0.866	(330, 0.866)
360	1	(360, 1)

# Graph Cos(x)

Notes p. 21



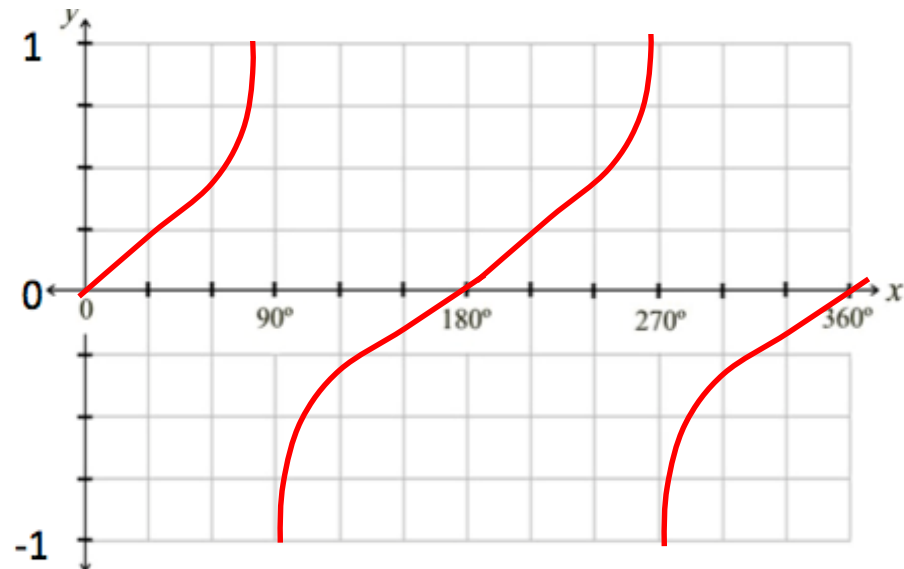
Complete the table below:

Degree	Tan(x)	Point (Degree, Tan(x))
0	0	(0, 0)
30	0.577	(30, 0.577)
60	1.73	(60, 1.73)
90	Undefined	
120	-1.73	(120, -1.73)
150	-0.577	(150, -0.577)
180	0	(180, 0)
210	0.577	(210, 0.577)
240	1.73	(240, 1.73)
270	Undefined	
300	-1.73	(300, -1.73)
330	-0.577	(330, -0.577)
360	0	(360, 0)

# Graph Tan(x)

Notes p. 22

What happens to tangent at  $90^\circ$  and  $270^\circ$ ? Why is this happening?



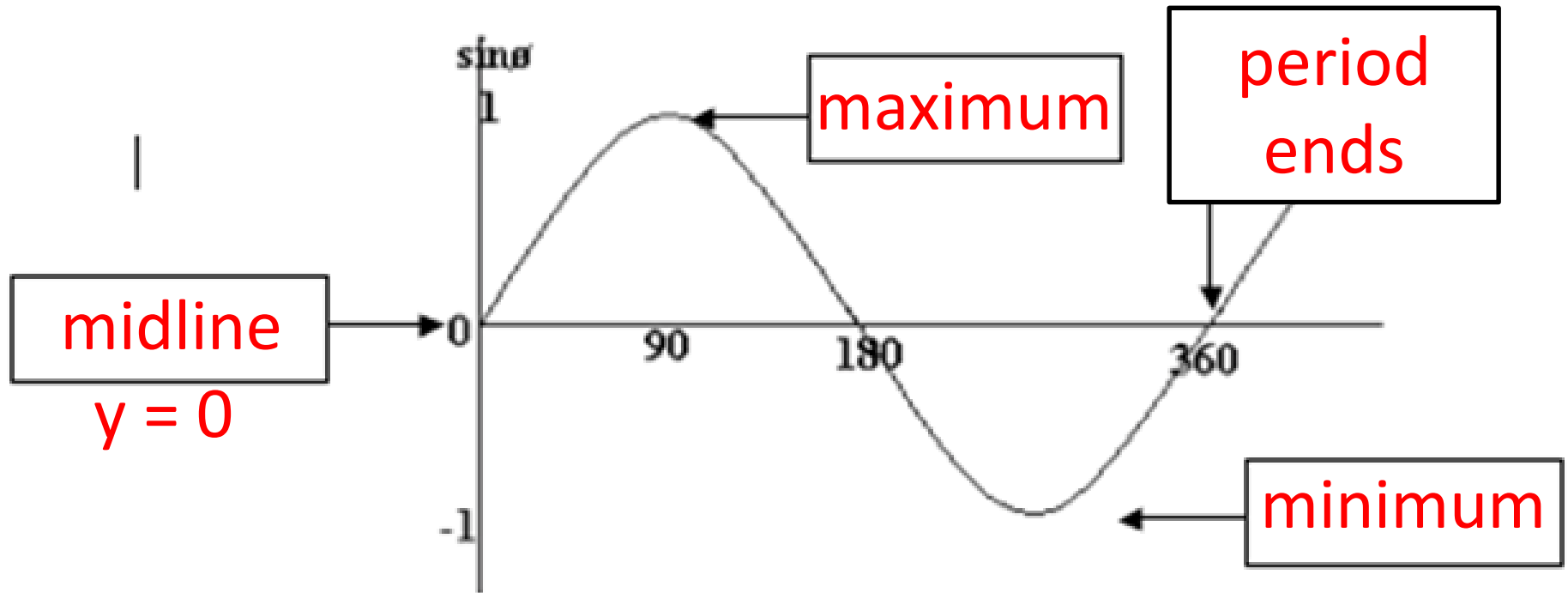


# Notes p. 23-24

## Graphs of Trig Functions

By each graph in your notes,  
fill in some of the key features  
as we discuss them on the next slides

## I. Sine Graph



a. Sine is increasing:

$$(0, 90) \cup (270, 360)$$

b. Sine is decreasing:

$$(90, 270)$$

c. Sine is positive:

$$(0, 180)$$

d. Sine is negative:

$$(180, 360)$$

# Plot of Sine

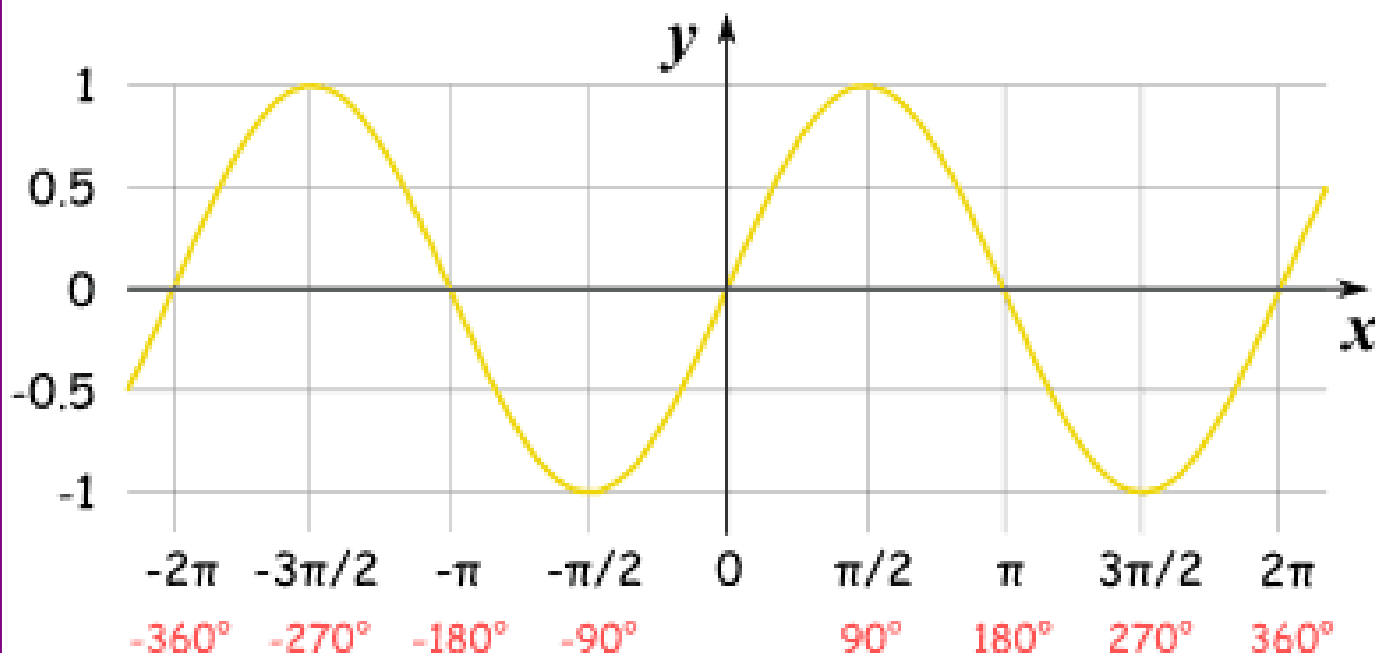
This exact graph is not in your Notes. Write these comments beside the graph in your notes!

The Sine Function has this beautiful up-down curve (which repeats every  $2\pi$  radians, or  $360^\circ$ ).

It starts at **0**, heads up to **1** by  $\pi/2$  radians ( $90^\circ$ ) and then heads down to **-1**.

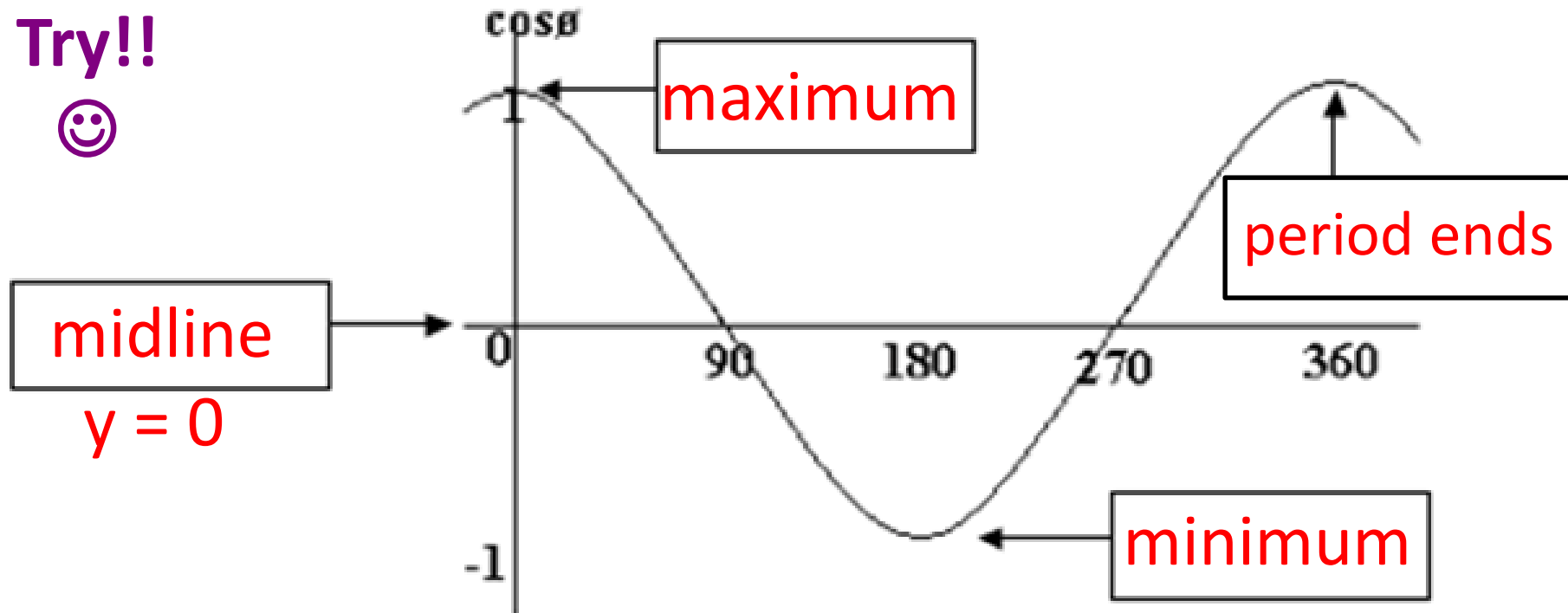
**Sine has a hill and a valley!**

**This graph has one cycle in the negative direction and one cycle in the positive direction.**



You  
Try!!  
😊

## II. Cosine Graph



a. Cosine is increasing:

$(180, 360)$

b. Cosine is decreasing:

$(0, 180)$

c. Cosine is positive:

$(0, 90) \cup (270, 360)$

d. Cosine is negative:  $\therefore$

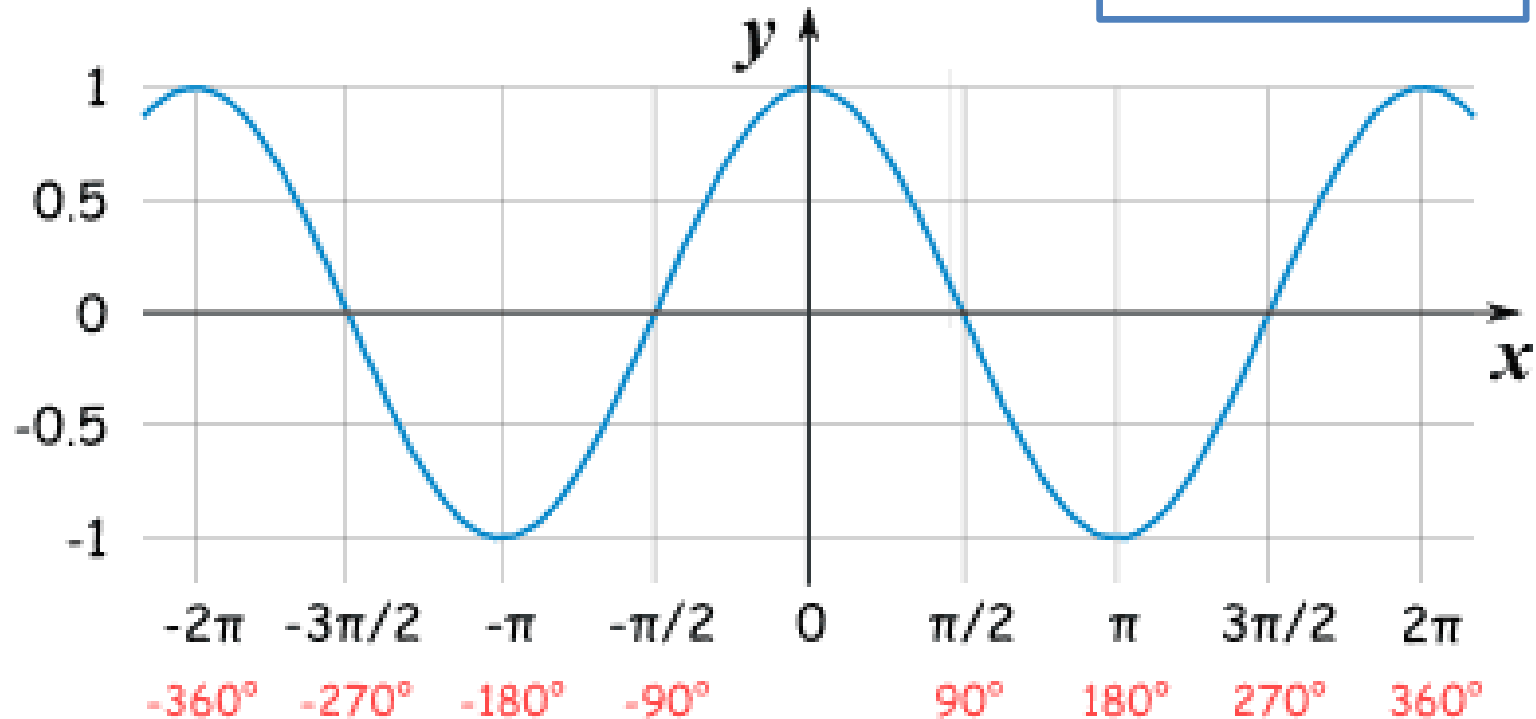
$(90, 270)$

**This exact graph is not in your Notes. Write these comments beside the graph in your notes!**

## Plot of Cosine

Cosine is just like Sine, but it starts at 1 and heads down until  $\pi$  radians ( $180^\circ$ ) and then heads up again.

**Cosine has one big valley!**



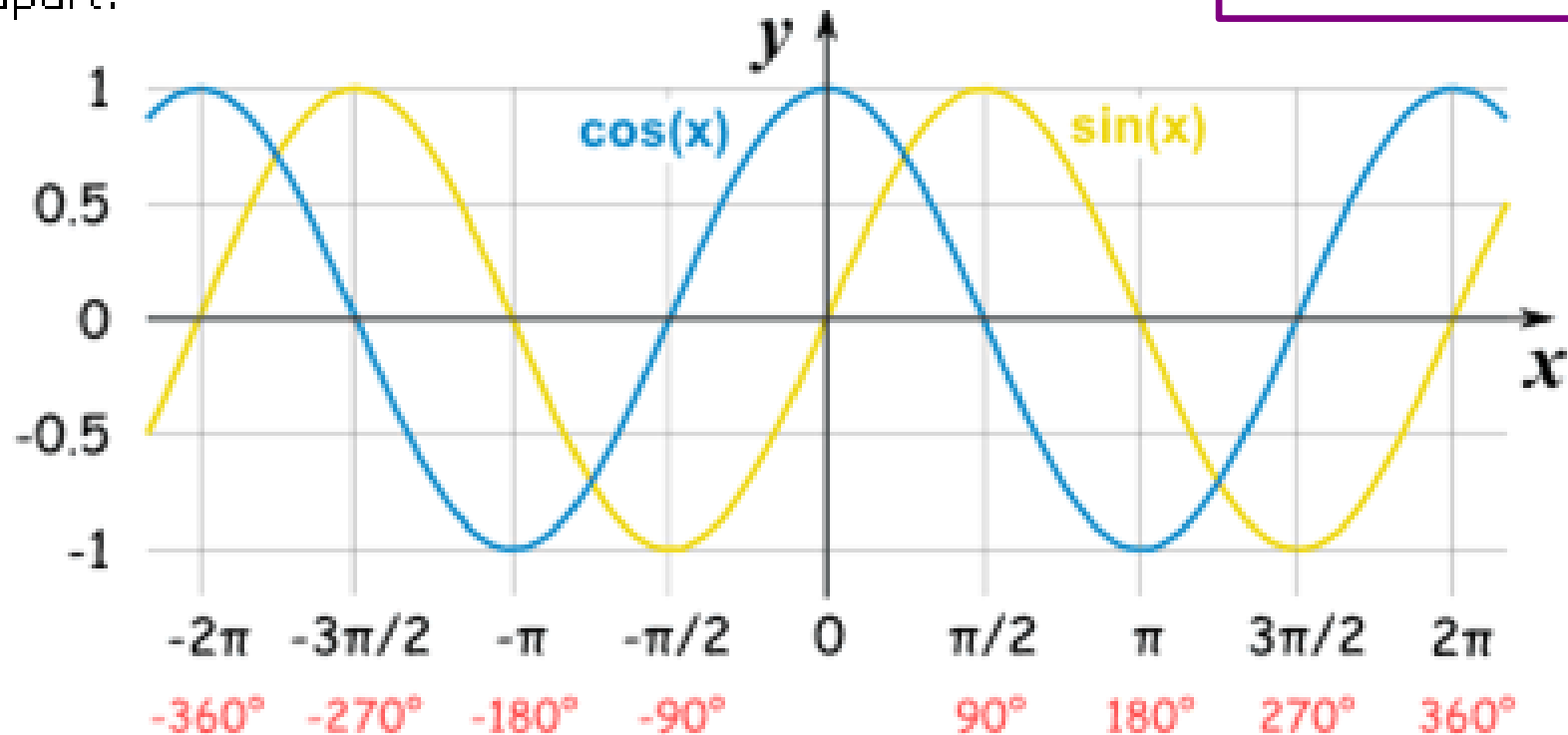
**This graph has one cycle in the negative direction and one cycle in the positive direction.**

# Graphs of Sine, Cosine and Tangent

## Plot of Sine and Cosine

In fact Sine and Cosine are like **good friends**: they follow each other, exactly " $\pi/2$ " radians, or  $90^\circ$ , apart.

How are Sine and Cosine graphs related?

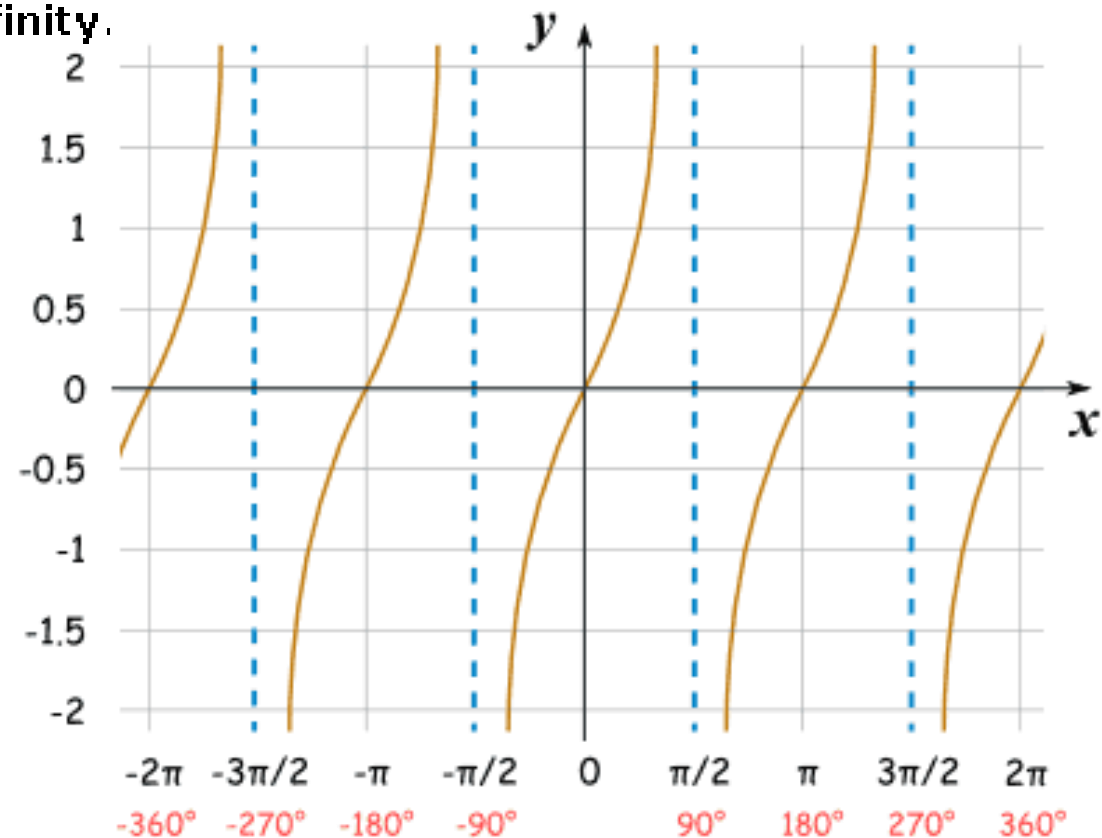


Sine and Cosine are Translations of each other by 90 degrees!

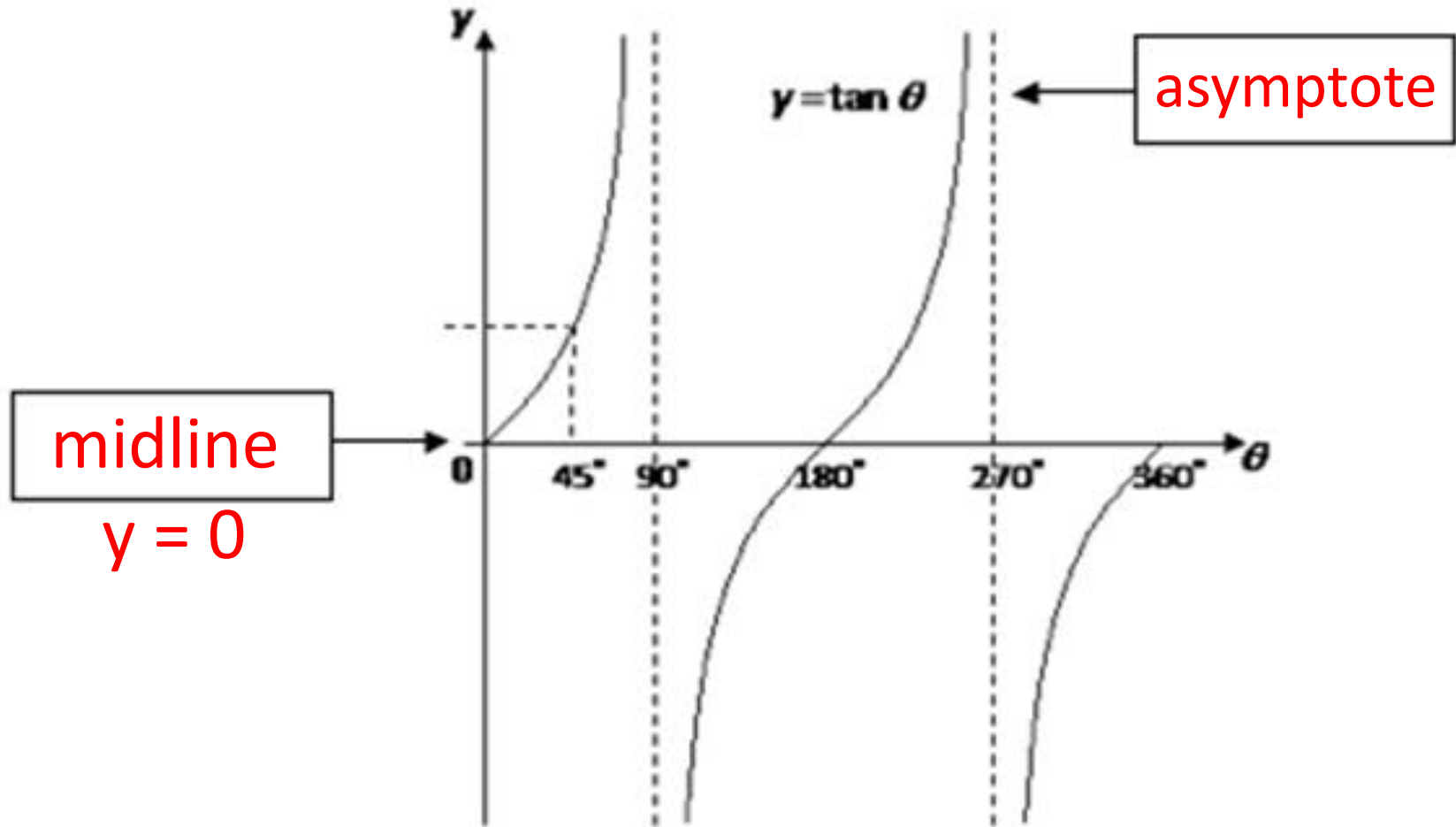
# Plot of the Tangent Function

The Tangent function has a completely different shape ... it goes between negative and positive Infinity, crossing through 0 (every  $\pi$  radians, or  $180^\circ$ ), as shown on this plot.

At  $\pi/2$  radians, or  $90^\circ$  (and  $-\pi/2$ ,  $3\pi/2$ , etc) the function is officially **undefined**, because it could be **positive Infinity** or **negative Infinity**.



### III. Tangent Graph



a. Tangent is increasing:

$(0, 90) \cup (90, 270) \cup (270, 360)$

c. Tangent is positive:

$(0, 90) \cup (180, 270)$

b. Tangent is decreasing:

never

d. Tangent is negative:

$(90, 180) \cup (270, 360)$

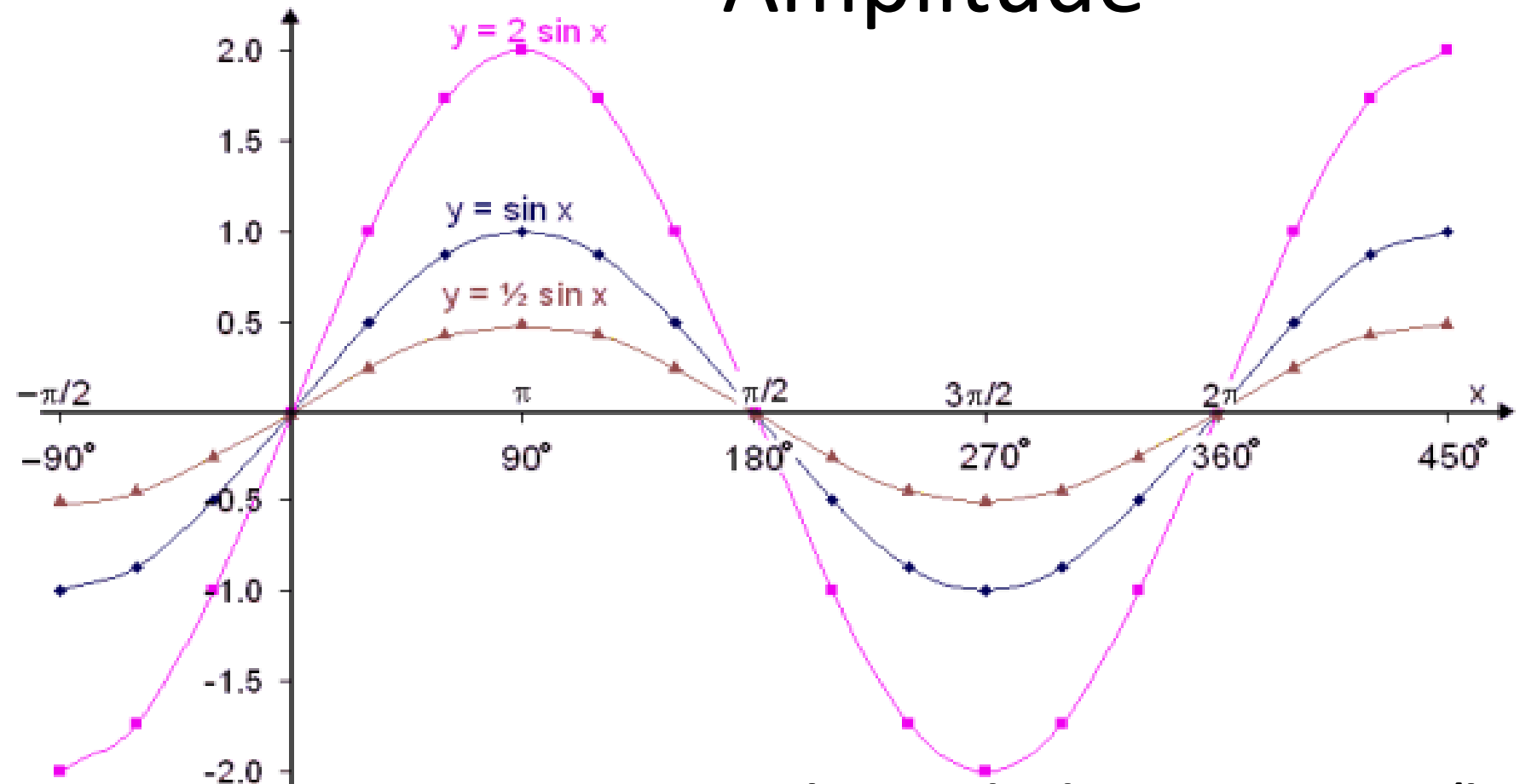


# Day 9 Notes continued

## Amplitudes, Midlines, and Period

Notes p. 24-27

# Amplitude



Given the standard equation  $y = a \sin(bx)$ ,  
how does “a” affect the graph?

What are the similarities  
and differences between  
the 3 graphs??

The “a” affects the height  
of the graph.

# Summary:

## Amplitude:

a. Amplitude is the height of the graph from the midline

b. A graph in the form of:

$$\underline{y = a \sin [b(x - c)] + d} \quad \text{and} \quad \underline{y = a \cos [b(x - c)] + d}$$

has an amplitude of  $|a|$ .

c. The amplitude of a standard sine or cosine graph is 1.

- d. The amplitude of a sine or cosine graph can be found using the following formula:

$$\text{amplitude} = |a| = \left| \frac{\text{max} - \text{min}}{2} \right|$$

- e. Find the amplitude for each of the following:

1.  $y = 3\sin x$      $\text{amp} = |3| = 3$

2.  $y = -4\cos 5x$      $\text{amp} = |-4| = 4$

3.  $y = (1/3)\sin x + 5$      $\text{amp} = \left| \frac{1}{3} \right| = \frac{1}{3}$

# Summary continued

## Midline:

The midline is the line that “cuts the graph in half.”

The midline is halfway between the max and the min.

The midline can be found by using the following formula:

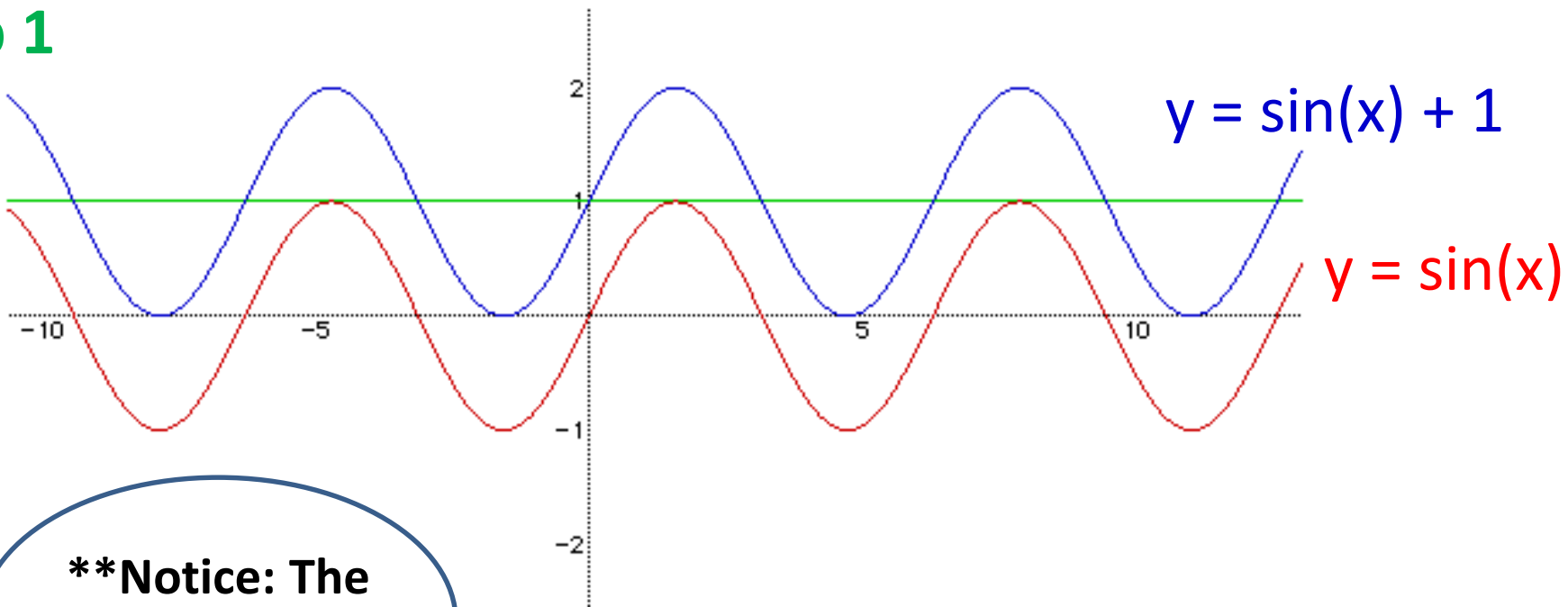
$$\text{Midline is } y = \frac{\text{Max} + \text{Min}}{2} \quad \text{OR} \quad y = \text{Min} + \text{Amp}$$

When there is no vertical shift, the midline is always the x-axis ( $y = 0$ ).

(Ex:  $y = \sin(x)$ ,  $y = 2\sin(x)$ ,  $y = \sin(3x)$  all have a midline of  $y = 0$  )

# Midline Continued

Midline  
moved  
up 1



**\*\*Notice: The  
amplitude did not  
change.**

# Period of a Function


**\*Period is the length of 1 cycle.\***

$Y = \sin(x)$  has a period of 360.

$y = \cos(x)$  has a period of 360.

$y = \tan(x)$  has a period of 180.

$$f(x) = A \sin(Bx)$$

$$Per = \frac{2\pi}{|B|} = \frac{360^\circ}{|B|}$$


**Note: this version of the formula is in radians, which is not a focus in math 2**

$$f(x) = A \sin(Bx) \quad \text{Per} = \frac{2(180)}{|B|} = \frac{360^\circ}{|B|}$$

Think of the pi as 180 degrees!!!

$$y = \sin x; \text{period} = \frac{360^\circ}{1} = 360^\circ$$

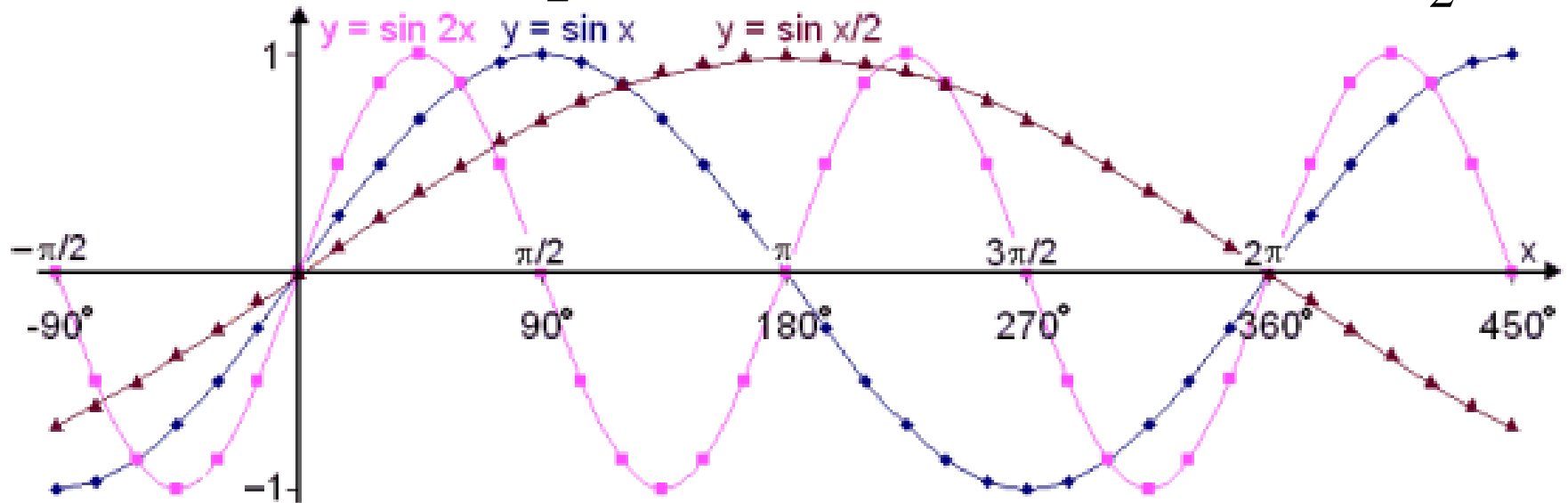
$$y = \cos x; \text{period} = \frac{360^\circ}{1} = 360^\circ$$

$$y = \sin\left(\frac{1}{2}x\right); \text{per} = \frac{360^\circ}{(1/2)} = 720^\circ$$

$$y = \cos\left(\frac{1}{2}x\right); \text{per} = \frac{360^\circ}{(1/2)} = 720^\circ$$

$$y = \sin(2x); \text{per} = \frac{360^\circ}{2} = 180^\circ$$

$$y = \cos(2x); \text{per} = \frac{360^\circ}{2} = 180^\circ$$





# Let's Graph one together! Notes pg. 26

We'll graph one period in the positive direction and one period in the negative direction.

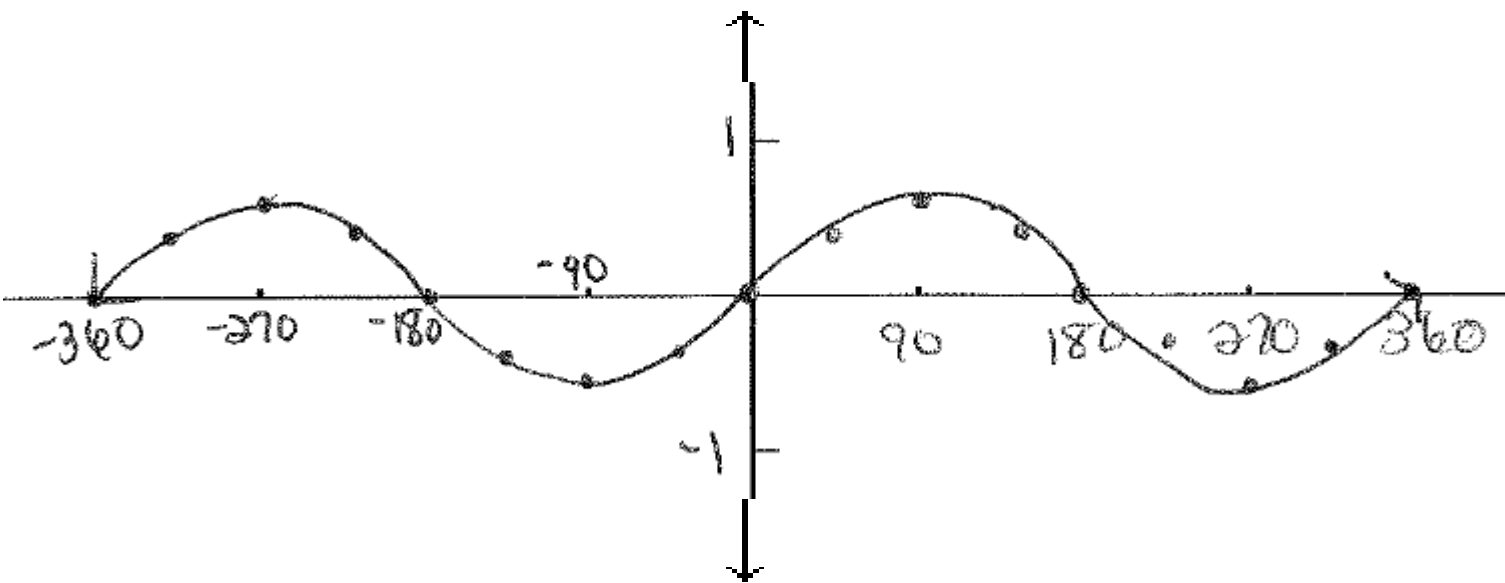
**\*\*TIP: divide each period into 8 even sections AND use the ASK feature in the calculator!\***  
**(2<sup>nd</sup> Window Indep -> ASK)**

4.  $y = 0.5 \sin(x)$

Amplitude: 0.5

Midline:  $y = 0$

Period:  $360^\circ$



Always find the period before graphing!

Label both axes!

# Practice – you try the others!

**Notes pg. 26-27 #5, 6, 7**

For each problem:

- \*graph **one period** in the positive direction and
- \***one period** in the negative direction.

**Remember to label the axes!**

- \***HINT: divide each period into 8 even sections AND use the ASK feature in the calculator!\***

# Practice Answers

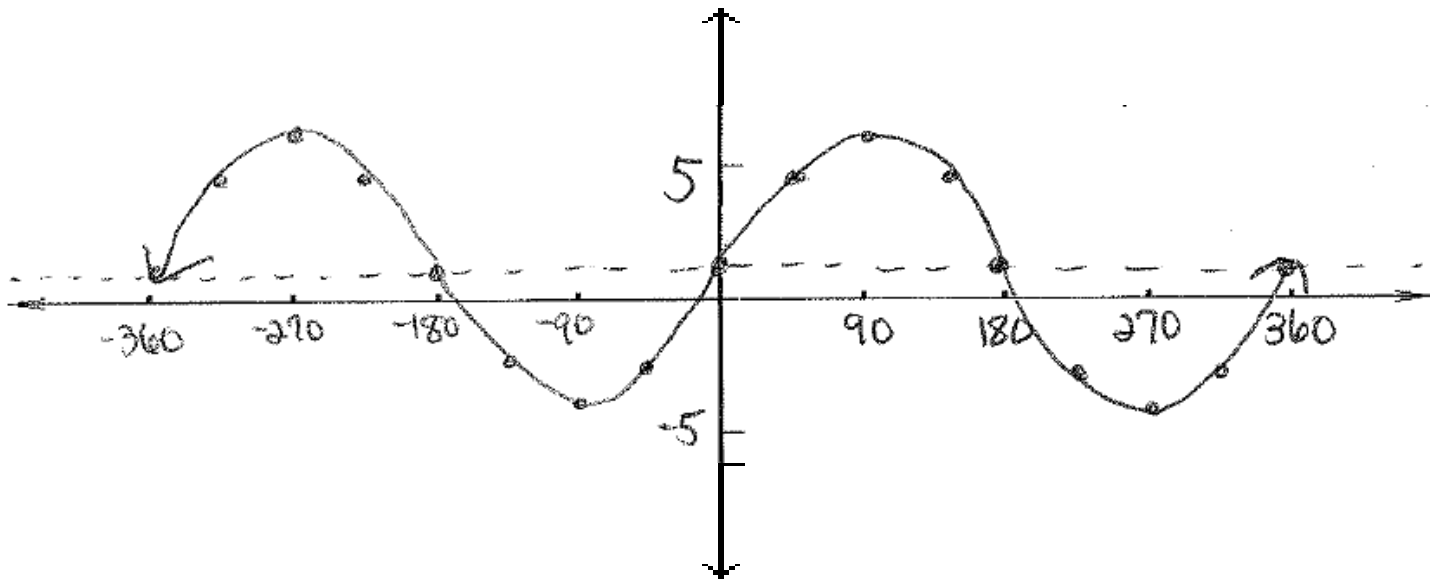
Graph one period in the positive direction and one period in the negative direction.

5.  $y = 5 \sin(x) + 1$

Amplitude: 5

Midline:  $y = 1$

Period:  $360^\circ$



Always  
find the  
period  
before  
graphing!

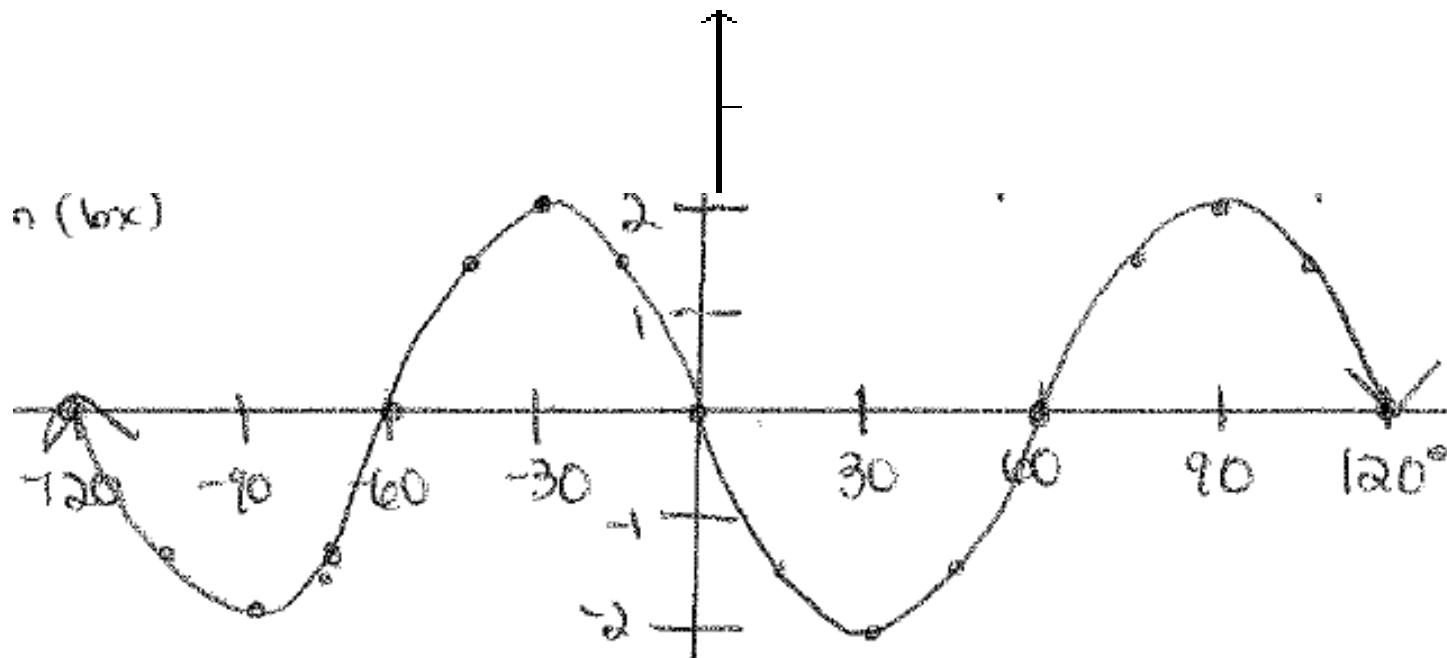
Label both  
axes!

# Practice Answers

Graph one period in the positive direction and one period in the negative direction.

6.  $y = -2 \sin(3x)$

Amplitude: 2      Midline:  $y = 0$       Period:  $120^\circ$



Always  
find the  
period  
before  
graphing!

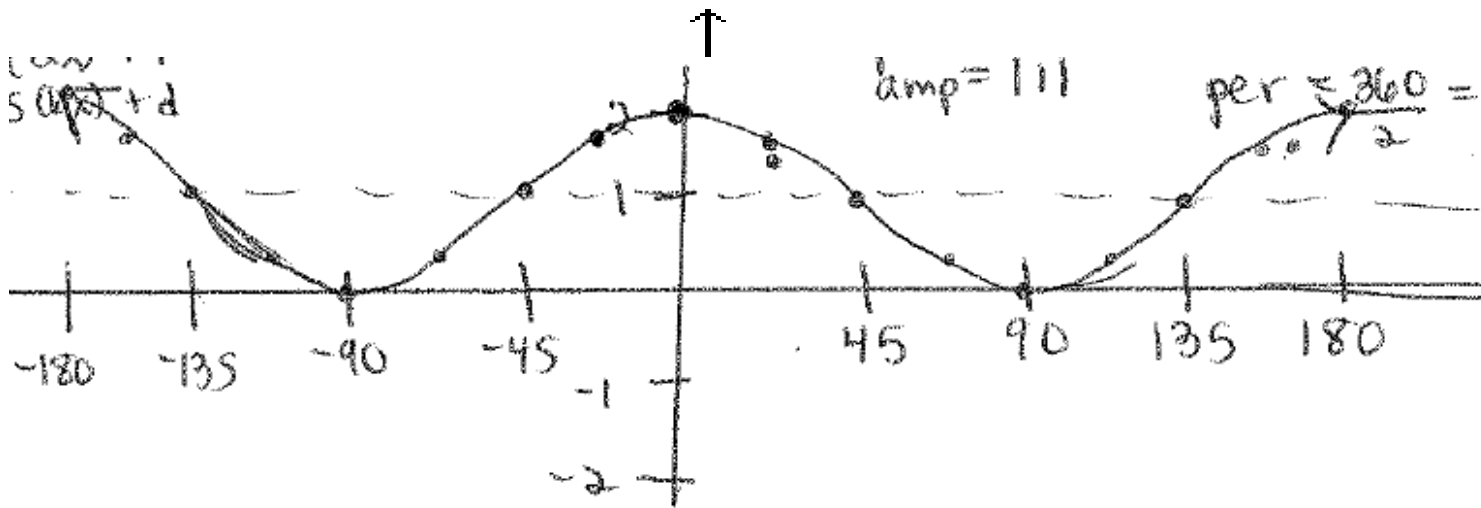
Label both  
axes!

# Practice Answers

We'll graph one period in the positive direction and one period in the negative direction.

7.  $y = \cos(2x) + 1$

Amplitude: 1      Midline:  $y = 1$       Period:  $180^\circ$



Always  
find the  
period  
before  
graphing!

Label both  
axes!