## Unit 5 Day 5:

## Law of Sines and the

Ambiguous Case

## Warm Up: Day 5

Draw a picture and solve. Label the picture with numbers and words including the angle of elevation/depression and height/length.

1. The straight line horizontal distance between a window in a school building and a skyscraper is 600 ft . From a window in the school, the angle of elevation to the top of the skyscraper is 38 degrees and the angle of depression to the bottom of the tower is 24 degrees.

Approximately how tall is the skyscraper?
2. A communications tower is located on a plot of flat land. It is supported by several guy wires.

You measure that the longest guy wire is anchored to the ground 112 feet from the base of the tower and that it makes an $76^{\circ}$ angle with the ground.

How long is the longest guy wire and at what height is
 it connected to the tower?

## Warm-Up: Day 5 ANSWER

1. The straight line horizontal distance between a window in a school building and a skyscraper is 600ft. From a window in the school, the angle of elevation to the top of the skyscraper is 38 degrees and the angle of depression to the bottom of the tower is 24 degrees. Approximately how tall is the skyscraper?

$$
\begin{aligned}
& \tan (38)=\mathrm{t} / 600 \\
& \mathrm{t}=600 \mathrm{tan}(38) \\
& \mathrm{t}=468.77 \mathrm{ft} \\
& \tan (24)=\mathrm{b} / 600 \\
& \mathrm{~b}=600 \mathrm{tan}(24) \\
& \mathrm{b}=267.14 \mathrm{ft} \\
& \\
& \text { Height }=\mathrm{t}+\mathrm{b} \\
& =735.91 \mathrm{ft}
\end{aligned}
$$

## Warm-Up: Day 5 ANSWERS

2. A communications tower is located on a plot of flat land. It is supported by several guy wires.

You measure that the longest guy wire is anchored to the ground 112 feet from the base of the tower and that it makes an $76^{\circ}$ angle with the ground.

How long is the longest guy wire and at what height is it connected to the tower?

$$
\begin{aligned}
& \tan (76)=\mathrm{t} / 112 \\
& \mathrm{t}=112 \tan (76) \\
& \text { tower }=449.2 \mathrm{ft} \\
& \cos (76)=112 / \mathrm{w} \\
& \mathrm{w}=112 / \cos (76) \\
& \text { wire }=462.96 \mathrm{ft}
\end{aligned}
$$

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## 1. $24.0 \mathrm{~cm}^{2} \quad$ 3. $11.9 \mathrm{yd}^{2}$

5. $1.0 \mathrm{yd}^{2} \quad$ 7. $12.6 \mathrm{~cm}^{2}$
6. $37.6 \mathrm{~m}^{2} \quad 11.55 .4 \mathrm{~km}^{2} \quad$ 13. $9.7 \mathrm{~mm}^{2}$
7. $54.5 \mathrm{~cm}^{2} \quad$ 17. $80.9 \mathrm{~m}^{2}$

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1. $101^{\circ}, 41.1,52.6$

$$
\text { 4. } 19^{\circ}, 179.37,90.85
$$

2. $98^{\circ}, 15.49,44.86$
3. $83^{\circ}, 24.1,10.2$
4. Perimeter $=89.7$

## Homework

## Packet p. 9

## Start studying for the quiz! Have you made flash cards for studying the formulas?

## For Today's Notes

We're doing longer problems with multiple diagrams and multiple triangles possible, so

You Need

- Notes Printout
- AND Notebook Paper


## The Ambiguous Case:

If two sides and an angle opposite one of them is Given (SSA), three possibilities can occur.
(1) No such triangle exists.
(2) Exactly one triangle exists.
(3) Two different triangles exist.

## The Ambiguous Case:

Before we look at the cases, let's use what we know about right triangles to set up the ratio for the following triangle.

$$
\sin \mathbf{A}=\frac{h}{b}
$$



When we solve for $\mathbf{h}$, we get $\mathbf{h}=\underline{b \cdot \sin A}$

| Figures | a |  |  |
| :--- | :---: | :---: | :---: |
| Number of <br> Triangles <br> Possible | $\mathrm{a}<\mathrm{h}$ | $\mathrm{a}=\mathrm{h}$ | $\mathrm{a}>\mathrm{h}$ <br> And $\mathrm{a}<\mathrm{b}$ |
| Occurs when.... |  |  |  |

Summary:
If the side across from the given angle is smaller than the other side AND it is a SSA scenario, then check for the ambiguous case!

Use a separate piece Law of Sines of paper to write examples!! Ambiguous Case (SSA)

## Example 1:

Solve $\triangle A B C$ if $m \angle A=25^{\circ}, a=125$, and $b=150$. Round to the nearest tenth.

$$
\begin{array}{ll}
\text { Case 1: } & \text { Case 2: } \\
\mathrm{m} \angle \mathrm{C}=124.5^{\circ} & \mathrm{m} \angle \mathrm{C}=5.5^{\circ} \\
\mathrm{m} \angle B=30.5^{\circ} & \mathrm{m} \angle B=149.5^{\circ} \\
\mathrm{c}=243.8 & \mathrm{c}=28.3
\end{array}
$$

## Law of Sines Ambiguous Case (SSA)

## Example 2:

Solve a triangle when one side is 27 meters, another side is 40 meters and a non-included angle across from the $\mathbf{2 7}$ meter side is $33^{\circ}$. Round to the nearest tenth.

$$
\begin{array}{ll}
\text { Case 1: } & \text { Case 2: } \\
\mathrm{m} \angle \mathrm{C}=93.2^{\circ} & \mathrm{m} \angle \mathrm{C}=20.8^{\circ} \\
\mathrm{m} \angle B=53.8^{\circ} & \mathrm{m} \angle B=126.2^{\circ} \\
\mathrm{c}=49.5 & \mathrm{c}=17.6
\end{array}
$$

## You Try! Law of Sines Ambiguous Case (SSA)

Example 3: $m \angle C=48, c=93, b=125$
Round to the nearest tenth.

$$
\begin{array}{ll}
\text { Case 1: } & \text { Case 2: } \\
\mathrm{B}=87.3^{\circ} & \mathrm{B}=92.7^{\circ} \\
\mathrm{A}=44.7^{\circ} & \mathrm{A}=39.3^{\circ} \\
\mathrm{a}=88.0 & \mathrm{a}=79.3^{\circ}
\end{array}
$$

# You Try! Law of Sines Ambiguous Case (SSA) 

Example 4: $\mathrm{m} \angle \mathrm{A}=24, \mathrm{a}=9.8, \mathrm{~b}=17$
Round to the nearest tenth.

## You Try! Law of Sines Practice p. 14-15

Round to the nearest tenth.

1. For $\triangle \mathrm{DEF}$,
$e=52, f=41$, and $\mathrm{m} \angle F=48^{\circ}$. Find all possible $\mathrm{m} \angle E$ to the nearest degree.


F
$\mathrm{m} \angle \mathrm{E}=70.5^{\circ}$ or $109.5^{\circ}$
3. For $\triangle \mathrm{ABC}$,
$b=120, c=92$, and $\mathrm{m} \angle C=42^{\circ}$. How many triangles can be formed?
2. For $\triangle \mathrm{LMN}$,
$l=27, m=15$, and $m \angle L=55^{\circ}$. Find all possible $\mathrm{m} \angle M$ to the nearest degree.


$$
\mathrm{m} \angle \mathrm{M}=27.1^{\circ}
$$

4. For $\triangle \mathrm{DEF}$,
$d=6, e=24$, and $\mathrm{m} \angle E=38^{\circ}$. How many Triangles can be formed?

$\mathrm{m} \angle \mathrm{D}=8.9^{\circ}$

## You Try! Law of Sines Practice p. 14-15

 6-7 Round to the nearest tenth.5. For triangle $D E F, d=25, e=30$, and $m \angle E=40^{\circ}$. Find all possible measurements of $f$ to the nearest whole number.

$$
f=44.48, \quad \text { so } f \approx 44
$$

6. Given with , $b=15 \mathrm{~cm}$, and , solve the triangle.

$$
\begin{array}{ll}
\text { Case 1: } & \text { Case 2: } \\
C=48.2^{\circ} & C=131.8^{\circ} \\
A=97.8^{\circ} & A=14.2^{\circ} \\
a=26.6 & a=6.6
\end{array}
$$


7. Given triangle $A B C, a=8, b=10$, and $m \angle A$ : the triangle.

$$
\begin{array}{ll}
\text { Case 1: } & \text { Case 2: } \\
B=44.3^{\circ} & B=135.7^{\circ} \\
C=101.7^{\circ} & C=10.3^{\circ} \\
C=14.0 & C=2.6
\end{array}
$$

## Puzzle Time!

## Law of Sine

## What do you call an unemployed jester?



## Homework

## Packet p. 9

## Start studying for the QUIZ!

